Formal Methods in Software Development Exercise 5 (December 9)

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The result is to be submitted by the deadline stated above *via the Moodle interface* of the course as a .zip or .tgz file which contains

- 1. a PDF file with
 - a cover page with the course title, your name, Matrikelnummer, and email address,
 - a section for each part of the exercise with the requested deliverables and optionally any explanations or comments you would like to make;
- 2. the RISCAL specification (.txt) file(s) used in the exercise;
- 3. the .java/.theory file(s) used in the exercise,
- 4. the task directory (.PETASKS*) generated by the RISC ProgramExplorer.

Email submissions are not accepted.

Exercise 5a (30P): Proving Verification Conditions

Take the five verification conditions A, B1, B2, C, D manually derived in Exercise 4 and checked there with RISCAL (if you did not solve that exercise, you may ask a colleague for these conditions or take them from the distributed sample solution).

The goal of this exercise is to *prove* these conditions with the help of the RISC ProofNavigator (in the style of the verification of the "linear search" algorithm presented in class) for arrays of *arbitrary* length n > 0 and non-negative integer elements of *arbitrary* size.

For this purpose, write a declaration file with the following structure

```
newcontext "exercise5a";

// arrays as presented in class (except ELEM = INT)
ELEM: TYPE = INT;
...

// program variables and mathematical constants
a: ARR; n: INT;
...
```

In this formalization, extend pre-, post-condition, and invariant by the formula n = length(a) (which implies n >= 0); again you may omit clauses that state that a and n remain unchanged.

All proofs can be performed with the commands expand, scatter, instantiate, split, and auto (it may be sometimes wise to use the goal command to switch the goal formula).

The deliverables for this exercise consists of the following items:

- 1. a (nicely formatted) copy of the ProofNavigator file (included as text, not as screenshots);
- 2. for each proof of a formula F, a readable screenshot of the RISC ProofNavigator after executing the command proof F (displaying the proof tree) with explicit statements whether the proof succeeded;
- 3. if any check gives an error respectively any proof fails, a detailed explanation of the estimated reason of the failure.

Exercise 5b (70P): Verifying a Program by Checking and Proving

Similar to Exercise 1, we consider the following problem: given an array a of n non-negative integer elements, find the index p of the maximum element of a. However, now n=0 is also allowed; if n=0, then p shall be -1. The goal of this exercise is to take the following Java program that solves this problem, and to use the RISC ProgramExplorer to annotate the program with specification and annotations, analyze its semantics, and verify its correctness with respect to its specification:

```
class Exercise5
 // returns index of maximum element in array a
  // of non-negative integers (-1, if a is empty)
  public static int maximum(int[] a)
    int n = a.length;
    if (n == 0)
      return -1;
    else
      int p = 0;
      int m = 0;
      int i = 0;
      while (i < n)
        if (a[i] > m)
        {
          p = i;
          m = a[i];
        i = i+1;
      }
      return p;
    }
  }
}
```

In detail, perform the following tasks:

- (20P) For a first validation of specification and invariants, take the RISCAL specification file maximum.txt which embeds an algorithmic version of above code in a procedure maximumIndex and equip this procedure with suitable pre-conditions, post-conditions, invariants, and termination term. Validate (for moderately large values N > 0 and M > 0) the annotations (check the procedure and check the derived verification conditions). These validated annotations shall then serve as the basis of the further proof-based verification.
- 2. (20P) Create a separate directory in which you place the file Exercise5.java that contains above Java procedure, cd to this directory, and start ProgramExplorer & from there. The task directory .PETASKS* is then generated as a subdirectory of this directory. (If you use the virtual course machine, place the directory for this exercise into the home directory of the guest user; in particular, do not place it into the directory shared with the host computer).

Specify the method by an appropriate contract (clauses requires, assignable, and ensures) and annotate the loop with an appropriate invariant and termination term (do not forget the non-null status of the array). In contrast to RISCAL, you have to specify here also all available information you have from the precondition about the input array (because in Java procedure parameters are not constants).

Investigate the computed semantics (transition relation and termination condition) of the method and give an informal interpretation of the semantics (and your explanation whether respectively why it seems adequate) in sufficient detail.

3. (30P) Verify all (non-optional) tasks generated from the method. Only few of them should require interactive proofs; most of these can probably be performed just by application of decompose, split, scatter and auto.

The only more complex cases should be the proofs that the invariant is preserved and that the method body ensures the postcondition; here it is wise to first perform a decompose and then a split corresponding to the two branches in the method respectively the loop body (if you immediately perform a scatter, you have to make a split in each of the resulting proof obligations which considerably blows up the proof).

The deliverables of this exercise consist of

- 1. a nicely formatted copy of the RISCAL specification (included as text, not as screenshots);
- 2. the outputs of the checks (included as text, not as screenshots) with explicit statements whether the checks succeeded;
- 3. a (nicely formatted) copy of the annotated . java file used in the exercise,
- 4. a screenshot of the corresponding "Semantics" view and an informal interpretation of the method semantics;
- 5. a screenshot of the "Analysis" view of the RISC ProgramExplorer with the specification/implementation of the method and the (expanded) tree of all (non-optional) tasks generated from the method,
- 6. for each task generated by the RISC ProgramExplorer an explicit statement whether the goal of the task was achieved or not and, if yes, how (fully automatic proof, immediate completion after starting an interactive proof, complete or incomplete interactive proof),
- 7. for each truly interactive proof, a screenshot of the corresponding "Verify" view with the proof tree.