# Verifying Java Programs with KeY

Wolfgang Schreiner
Wolfgang.Schreiner@risc.jku.at

Research Institute for Symbolic Computation (RISC)
Johannes Kepler University, Linz, Austria
http://www.risc.jku.at



## Verifying Java Programs

- Extended static checking of Java programs:
  - Even if no error is reported, a program may violate its specification.
    - Unsound calculus for verifying while loops.
  - Even correct programs may trigger error reports:
    - Incomplete calculus for verifying while loops.
    - Incomplete calculus in automatic decision procedure (Simplify).
- Verification of Java programs:
  - Sound verification calculus.
    - Not unfolding of loops, but loop reasoning based on invariants.
    - Loop invariants must be typically provided by user.
  - Automatic generation of verification conditions.
    - From JML-annotated Java program, proof obligations are derived.
  - Human-guided proofs of these conditions (using a proof assistant).
    - Simple conditions automatically proved by automatic procedure.

We will now deal with an integrated environment for this purpose.



## The KeY Tool

`http://www.key-project.org`

- KeY: environment for verification of JavaCard programs.
  - Subset of Java for smartcard applications and embedded systems.
  - Universities of Karlsruhe, Koblenz, Chalmers, 1998–
    - Beckert et al: "Deductive Software Verification – The KeY Book: From Theory to Practice", Springer, 2016.
    - "Chapter 16: Formal Verification with KeY: A Tutorial"
- Specification languages: OCL and JML.
  - Original: OCL (Object Constraint Language), part of UML standard.
  - Later added: JML (Java Modeling Language).
- Logical framework: Dynamic Logic (DL).
  - Successor/generalization of Hoare Logic.
  - Integrated prover with interfaces to external decision procedures.
    - Simplify, CVC3, CVC4, Yices, Z3.

Now only JML is supported as a specification language.



## Dynamic Logic

Further development of Hoare Logic to a modal logic.

- Hoare logic: two separate kinds of statements.
  - Formulas $P, Q$ constraining program states.
  - Hoare triples $\{P\}C\{Q\}$ constraining state transitions.
- Dynamic logic: single kind of statement.

  Predicate logic formulas extended by two kinds of modalities.

  - $[C]Q$ $(\Leftrightarrow \neg\langle C\rangle\neg Q)$
    - Every state that can be reached by the execution of $C$ satisfies $Q$.
    - The statement is trivially true, if $C$ does not terminate.
  - $\langle C\rangle Q$ $(\Leftrightarrow \neg[C]\neg Q)$
    - There exists some state that can be reached by the execution of $C$ and that satisfies $Q$.
    - The statement is only true, if $C$ terminates.

States and state transitions can be described by DL formulas.

## Dynamic Logic versus Hoare Logic

Hoare triple $\{P\}C\{Q\}$ can be expressed as a DL formula.

- Partial correctness interpretation: $P \Rightarrow [C]Q$
  - If $P$ holds in the current state and the execution of $C$ reaches another state, then $Q$ holds in that state.
  - Equivalent to the partial correctness interpretation of $\{P\}C\{Q\}$.
- Total correctness interpretation: $P \Rightarrow \langle C \rangle Q$
  - If $P$ holds in the current state, then there exists another state that can be reached by the execution of $C$ in which $Q$ holds.
  - If $C$ is deterministic, there exists at most one such state; then equivalent to the total correctness interpretation of $\{P\}C\{Q\}$.

For deterministic programs, the interpretations coincide.



## Advantages of Dynamic Logic

Modal formulas can also occur in the context of quantifiers.

- Hoare Logic: $\{x = a\}$ `y:=x*x` $\{x = a \wedge y = a^2\}$
  - Use of free mathematical variable $a$ to denote the "old" value of $x$.
- Dynamic logic: $\forall a : x = a \Rightarrow [\texttt{y:=x*x}]\ x = a \wedge y = a^2$
  - Quantifiers can be used to restrict the scopes of mathematical variables across state transitions.

Set of DL formulas is closed under the usual logical operations.



## A Calculus for Dynamic Logic

- A core language of commands (non-deterministic):

| | |
|---|---|
| $X := T$ | . . . assignment |
| $C_1; C_2$ | . . . sequential composition |
| $C_1 \cup C_2$ | . . . non-deterministic choice |
| $C^*$ | . . . iteration (zero or more times) |
| $F?$ | . . . test (blocks if $F$ is false) |

- A high-level language of commands (deterministic):

| | | |
|---|---|---|
| **skip** | = | true? |
| **abort** | = | false? |
| $X := T$ | | |
| $C_1; C_2$ | | |
| **if** $F$ **then** $C_1$ **else** $C_2$ | = | $(F?; C_1) \cup ((\neg F)?; C_2)$ |
| **if** $F$ **then** $C$ | = | $(F?; C) \cup (\neg F)?$ |
| **while** $F$ **do** $C$ | = | $(F?; C)^*; (\neg F)?$ |

A calculus is defined for dynamic logic with the core command language.



## A Calculus for Dynamic Logic

- Basic rules:
  - Rules for predicate logic extended by general rules for modalities.
- Command-related rules:
  - $\dfrac{\Gamma \vdash F[T/X]}{\Gamma \vdash [X := T]F}$
  - $\dfrac{\Gamma \vdash [C_1][C_2]F}{\Gamma \vdash [C_1; C_2]F}$
  - $\dfrac{\Gamma \vdash [C_1]F \quad \Gamma \vdash [C_2]F}{\Gamma \vdash [C_1 \cup C_2]F}$
  - $\dfrac{\Gamma \vdash F \Rightarrow [C]F}{\Gamma \vdash F \Rightarrow [C^*]F}$
  - $\dfrac{\Gamma \vdash F \Rightarrow G}{\Gamma \vdash [F?]G}$

From these, Hoare-like rules for the high-level language can be derived.

# Objects and Updates

Calculus has to deal with the pointer semantics of Java objects.

- Aliasing: two variables $o, o'$ may refer to the same object.
  - Field assignment $o.a := T$ may also affect the value of $o'.a$.
- Update formulas: $\{o.a \leftarrow T\}F$
  - Truth value of $F$ in state after the assignment $o.a := T$.
- Field assignment rule:

$$\frac{\Gamma \vdash \{o.a \leftarrow T\}F}{\Gamma \vdash [o.a := T]F}$$

- Field access rule:

$$\frac{\Gamma, o = o' \vdash F(T) \qquad \Gamma, o \neq o' \vdash F(o'.a)}{\Gamma \vdash \{o.a \leftarrow T\}F(o'.a)}$$

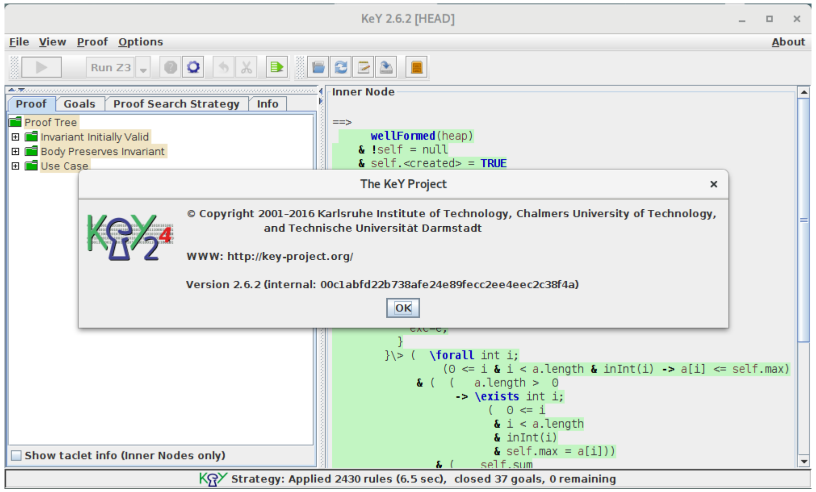
  - Case distinction depending on whether $o$ and $o'$ refer to same object.
  - Only applied as last resort (after all other rules of the calculus).

Considerable complication of verifications.



# The JMLKeY Prover

```
> KeY &
```






# A Simple Example

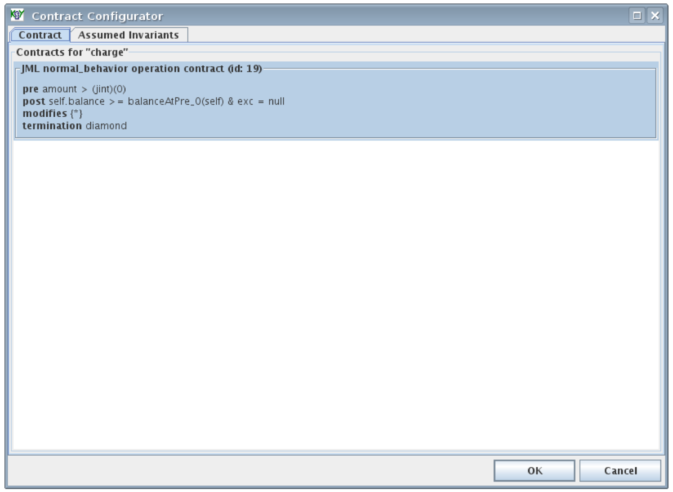
File/Load Example/Getting Started/Sum and Max

```
class SumAndMax {
  int sum; int max;
  /*@ requires (\forall int i;
    @   0 <= i && i < a.length; 0 <= a[i]);
    @ assignable sum, max;
    @ ensures (\forall int i;
    @   0 <= i && i < a.length; a[i] <= max);
    @ ensures (a.length > 0 ==>
    @   (\exists int i;
    @     0 <= i && i < a.length;
    @     max == a[i]));
    @ ensures sum == (\sum int i;
    @   0 <= i && i < a.length; a[i]);
    @ ensures sum <= a.length * max;
    @*/
  void sumAndMax(int[] a) {
    sum = 0;
    max = 0;
    int k = 0;
```

```
    /*@ loop_invariant
      @ 0 <= k && k <= a.length
      @ && (\forall int i;
      @      0 <= i && i < k; a[i] <= max)
      @ && (k == 0 ==> max == 0)
      @ && (k > 0 ==> (\exists int i;
      @       0 <= i && i < k; max == a[i]))
      @ && sum == (\sum int i;
      @       0 <= i && i< k; a[i])
      @ && sum <= k * max;
      @ assignable sum, max;
      @ decreases a.length - k;
      @*/
    while (k < a.length) {
      if (max < a[k]) max = a[k];
      sum += a[k];
      k++;
} } }
```

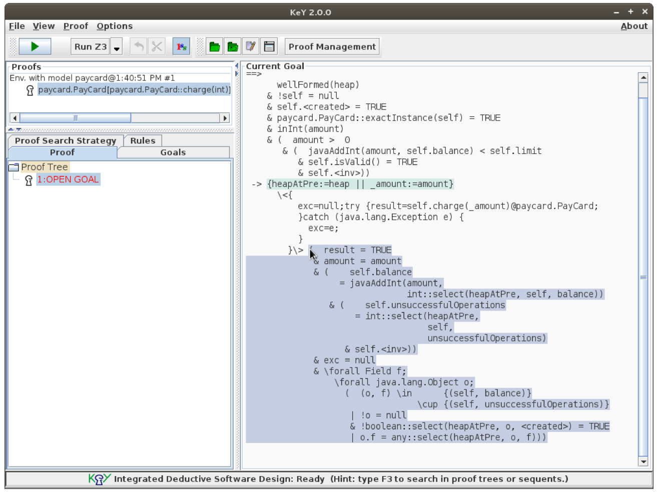


# A Simple Example (Contd)




Generate the proof obligations and choose one for verification.

# A Simple Example (Contd'2)




The proof obligation in Dynamic Logic.



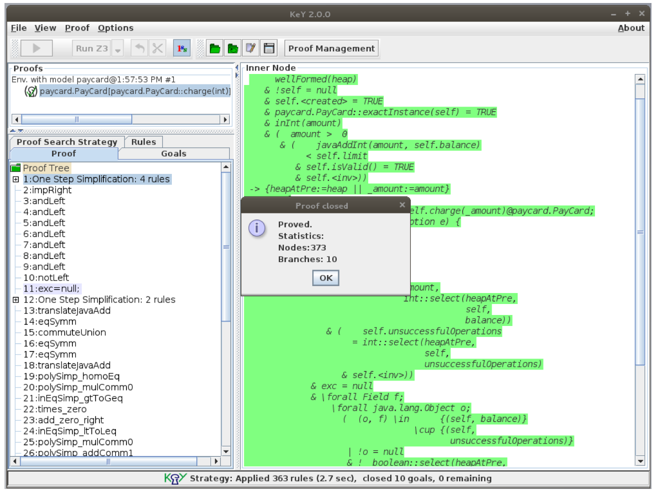
# A Simple Example (Contd'3)

```
 wellFormed(heap)
==>
      true
   & !self=null
   & ...
   & (\forall int i; (0 <= i & i < a.length & inInt(i) -> 0 <= a[i])
      &(self.<inv> & !a = null))
 -> {heapAtPre:=heap || _a:=a}
      \<{
          exc=null;try {
            self.sumAndMax(_a)@SumAndMax;
          } catch (java.lang.Throwable e){ exc=e; }
        }\>(\forall int i;
                  (0 <= i & i < a.length & inInt(i) -> a[i] <= self.max)
             & ((   a.length > 0
                 -> \exists int i;
                      (0 <= i & i < a.length & inInt(i) & self.max = a[i]))
                & (  self.sum = javaCastInt(bsum{int i;}(0, a.length, a[i]))
                   & (self.sum <= javaMulInt(a.length, self.max) & self.<inv>)))
             & exc = null
             & \forall Field f;
                 \forall java.lang.Object o;
                   (  (o, f) \in      {(self,SumAndMax::$sum)}
                             \cup {(self,SumAndMax::$max)}
                    | !o = null
                    & !o.<created>@heapAtPre = TRUE
                    | o.f = o.f@heapAtPre))
```

Press button "Start" (green arrow).



# A Simple Example (Contd'4)



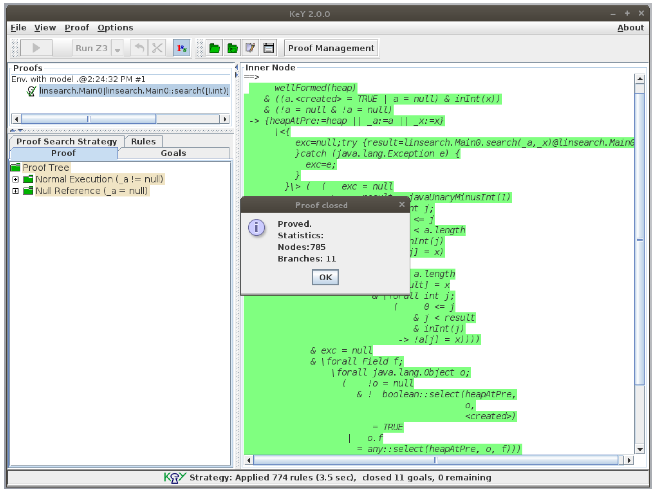

Proof runs through automatically.



# Linear Search

```
/*@ requires a != null;
  @ assignable \nothing;
  @ ensures
  @   (\result == -1 &&
  @     (\forall int j; 0 <= j && j < a.length; a[j] != x)) ||
  @   (0 <= \result && \result < a.length && a[\result] == x &&
  @     (\forall int j; 0 <= j && j < \result; a[j] != x));
  @*/
public static int search(int[] a, int x) {
  int n = a.length; int i = 0; int r = -1;
  /*@ loop_invariant
    @   a != null && n == a.length && 0 <= i && i <= n &&
    @   (\forall int j; 0 <= j && j < i; a[j] != x) &&
    @   (r == -1 || (r == i && i < n && a[r] == x));
    @ decreases r == -1 ? n-i : 0;
    @ assignable r, i; // required by KeY, not legal JML
    @*/
  while (r == -1 && i < n) {
    if (a[i] == x) r = i; else i = i+1;
  }
  return r;
}
```

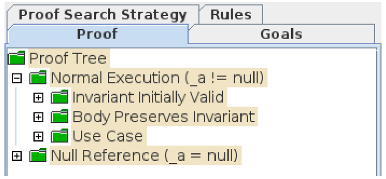
## Linear Search (Contd)




Also this verification is completed automatically.



## Proof Structure




- Multiple conditions:
  - Invariant initially valid.
  - Body preserves invariant.
  - Use case (invariant implies postcondition).
- If proof fails, elaborate which part causes trouble and potentially correct program, specification, loop annotations.

For a successful proof, in general multiple iterations of automatic proof search (button "Start") and invocation of separate SMT solvers required (button "Run Z3, Yices, CVC3, Simplify").



## Summary

- Various academic approaches to verifying Java(Card) programs.
  - Jack: http://www-sop.inria.fr/everest/soft/Jack/jack.html
  - Jive: http://www.pm.inf.ethz.ch/research/jive
  - Mobius: http://kindsoftware.com/products/opensource/Mobius/
- Do not yet scale to verification of full Java applications.
  - General language/program model is too complex.
  - Simplifying assumptions about program may be made.
  - Possibly only special properties may be verified.
- Nevertheless very helpful for reasoning on Java in the small.
  - Much beyond Hoare calculus on programs in toy languages.
  - Probably all examples in this course can be solved automatically by the use of the KeY prover and its integrated SMT solvers.
- Enforce clearer understanding of language features.
  - Perhaps constructs with complex reasoning are not a good idea...

In a not too distant future, customers might demand that some critical code is shipped with formal certificates (correctness proofs)...