Formal Methods in Software Development Exercise 1 (October 30)

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The result is to be submitted by the deadline stated above *via the Moodle interface* of the course as a .zip or .tgz file which contains

- 1. a PDF file with
 - a cover page with the course title, your name, Matrikelnummer, and email address,
 - a section for each part of the exercise with the requested deliverables and optionally any explanations or comments you would like to make;
- 2. the RISCAL specification (.txt) file(s) used in the exercise.

Email submissions are not accepted.

Exercise 1: Validating and Checking Program Specifications

We consider the following two problems:

- 1. Given an array a with n > 0 non-negative integer elements, find the maximum element m of a, i.e., the element m that occurs in a (i.e., at some index of a) and that is greater than or equal to all elements of a (i.e., the elements at all indices of a).
- 2. Given an array a with n > 0 non-negative integer elements, find the index p of the maximum element of a, i.e., a non-negative integer p less than n such that the element at p is greater than or equal to all elements of a (i.e., the elements at all indices of a).

In the RISCAL specification file maximum.txt you find two procedures maximumElement and maximumIndex that are supposed to solve these problems, respectively (but the procedures may contain bugs). The specification is based on two integer types index and elem that bound the domain of possible array indices respectively values by constants N and M respectively.

For *each* of the procedures perform the following tasks (the definitions already given in the specification file must *not* be modified unless explicitly noted):

- (a) Formalize the procedure's precondition and postcondition as predicates.
 - In the formulation, do not use the arithmetic quantifier max but only the predicate logic quantifiers \forall and \exists (translate above specification from natural language to logic). Hint: a formula ($\forall v:T$ with F. G) is equivalent to ($\forall v:T$. $F \Rightarrow G$) and a formula ($\exists v:T$ with F. G) is equivalent to ($\exists v:T$. $F \land G$); the former notation may be preferred.
- (b) Use the precondition and postcondition to implicitly define a function and check whether the computed results are as desired.
- (c) Formulate a theorem that states that some input satisfies the precondition and check this theorem.
- (d) Formulate a theorem that states that not every input satisfies the precondition and check this theorem.
- (e) Formulate a theorem that states that, for every input that satisfies the precondition, there exists some output that satisfies the postcondition, and check that theorem.
- (f) Formulate a theorem that states that, for every input that satisfies the precondition, not every output satisfies the postcondition, and check that theorem.
- (g) Formulate a theorem that states that, for every input that satisfies the precondition, the output is uniquely defined by the postcondition, and check that theorem.
- (h) Annotate the procedure with preconditions and postconditions and check the correctness of the procedure for all possible inputs; if a condition is a conjunction, it is recommended to use multiple annotation clauses.

Perform all checks with moderately large values N > 0 and M > 0.

Perform the function and theorem checks (b–g) with translation option "Nondeterminism" selected. If a theorem is not valid, give an explanation of why the theorem is not valid and whether this indicates an error in your specification or not. For this purpose, select the visualization option "Tree" and investigate the evaluation of the theorem.

Perform the procedure check (h) with translation option "Nondeterminism" *not* selected. If the execution of a procedure gives an error, give an explanation of why this is the case and whether this indicates an error in the procedure or not. For this purpose, select the visualization option "Trace" and investigate an execution of the procedure exhibiting the error. If the error indicates a bug in the procedure, fix this bug.

For running the visualizations in the RISCAL installation of the virtual machine, you have to start the software as RISCAL-visual &.

The deliverables for this exercise consists of the following items:

- 1. a nicely formatted copy of the extended specification (included as text, not as screenshots);
- 2. the outputs of the checks (included as text, not as screenshots);
- 3. if a check gives an error, a screenshot of the visualization exhibiting that error, an explanation of the error, and a justified statement that describes whether this indicates an error in your specifications or not;
- 4. if you fixed a bug in a procedure, a clear indication and explanation of that fix.