

Computer Systems (SS 2017)

Exercise 4: May 23, 2017

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The exercise is to be submitted by the denoted deadline via the submission interface of the Moodle course as a single file in zip (.zip) or tarred gzip (.tgz) format which contains the following files:

- A PDF file `ExerciseNumber-MatNr.pdf` (where *Number* is the number of the exercise and *MatNr* is your “Matrikelnummer”) which consists of the following parts:
 1. A decent cover page with the title of the course, the number of the exercise, and the author of the solution (identified by name, Matrikelnummer and email address).
 2. For every source file, a listing in a *fixed width font*, e.g. `Courier`, (such that indentations are appropriately preserved) and an appropriate *font size* such that source code lines do not break.
 3. A description of all tests performed (copies of program inputs and program outputs) explicitly highlighting, if some test produces an unexpected result.
 4. Any additional explanation you would like to give. In particular, if your solution has unwanted problems or bugs, please document these explicitly (you will get more credit for such solutions).
- Each source file of your solution (no object files or executables).

Please obey the coding style recommendations posted on the course site.

Exercise 4: Generic Polynomials by Inheritance

A univariate polynomial $\sum_{i=0}^n c_i \cdot x^i$ of degree n can be represented by an array of its $n + 1$ coefficients c_0, \dots, c_n . The goal of this exercise is to implement in this way a class `PolyInt` of univariate polynomials with integer coefficients. The implementation shall be based on a generic polynomial class `Polynomial` which works for arbitrary coefficient types that support the usual ring operations.

In more detail, the implementation shall work as follows:

1. Take the following abstract class `Ring`:

```
class Ring {
public:
    // destructor
    virtual ~Ring() {}

    // a heap-allocated copy of this element
    virtual Ring* copy() = 0;

    // the string representation of this element
    virtual string str() = 0;

    // the constant of the type of this element and the inverse of this element
    virtual Ring* zero() = 0;
    virtual Ring* operator-() = 0;

    // sum and product of this element and c
    virtual Ring* operator+(Ring* c) = 0;
    virtual Ring* operator*(Ring* c) = 0;

    // comparison function
    virtual bool operator==(Ring* c) = 0;
};
```

2. Implement a concrete class `Integer`

```
class Integer: public Ring {
public:
    // integer with value n (default 0)
    Integer(long n=0);
};
```

This class overrides all the abstract (pure virtual) operations of class `Ring` by concrete definitions for integer arithmetic (where integers are represented by `long` values).

Note that in the definition of the arithmetic and comparison functions the parameter `c` must be explicitly converted from type `Ring*` to type `Integer*`. Use the expression `dynamic_cast<Integer*>(c)` to receive a pointer to a `Integer` object (respectively `0`, if the conversion is not possible; the program may then be aborted with an error message).

3. Implement a concrete class Polynomial

```
class Polynomial: public Ring {
public:
    // polynomial with n>=0 coefficients and given variable name
    Polynomial(string var, int n, Ring **coeffs);

    // destructor
    virtual ~Polynomial();

    // evaluate this polynomial on c
    Ring* eval(Ring *c);
};
```

which implements univariate polynomials with generic coefficient types (i.e. coefficients that are represented by a concrete subclass of class Ring).

The class stores internally an array of the polynomial coefficients as Ring* values (i.e., pointers to objects of (a subclass of) class Ring) where the leading coefficient is not zero (the zero polynomial is represented by an array of length zero). The constructor thus ignores trailing zeros in the given arrays. The coefficient array is to be allocated on the heap and filled with the copy $r.\text{copy}()$ of every Ring element r of the given array; the destructor of the class thus frees these elements and the array. Please note that the constructor does neither store the array passed as an argument nor its elements!

Class Polynomial is itself a concrete subclass of Ring; it thus overrides the abstract (pure virtual) operations of class Ring by concrete definitions for polynomial arithmetic. The class also overrides the virtual destructor of class Ring to free the array that was allocated when the polynomial was constructed and its elements.

When adding/multiplying two polynomials, first allocate a temporary Ring* array for the coefficients of the result polynomial and then fill this array with the appropriate coefficients; finally construct the result polynomial from this array using the constructor and free the array. Do not forget to free temporary coefficient values that you have created but that are not needed any more.

Please note that class Polynomial does *not* use the class Integer described above!

The classes thus support the following operations:

```
Ring* c[] = { new Integer(-5), new Integer(2),
             new Integer(0), new Integer(-3) };
Polynomial* p = new Polynomial("x", 4, c);           // p = -3x^3 + 2x - 5
cout << p->str();
Integer* a =                                        // a = p(2)
    dynamic_cast<Integer*>(p->eval(new Integer(2)));
cout << a->str();
Polynomial* q =                                     // q = p+p
    dynamic_cast<Polynomial*>(p->operator+(p));
cout << q->str();
```

```
Polynomial* r = // r = p*q
    dynamic_cast<Polynomial*>(p->operator*(q));
cout << r->str();
```

Test class `Polynomial` in a *comprehensive* way (several calls of each function including the calls above); print the function results and show the output.