

**Problems Solved:**

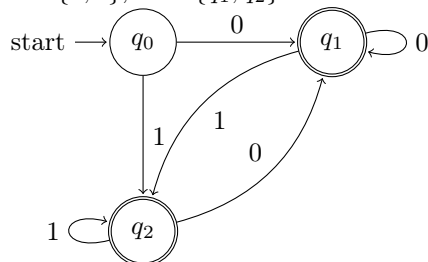
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**Name:**

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**Problem 6.** Let  $N = (Q, \Sigma, \delta, S, F)$  be the NFSM given by  $Q = \{q_0, q_1, q_2\}$ ,  $\Sigma = \{0, 1\}$ ,  $S = \{q_0\}$ ,  $F = \{q_1, q_2\}$ , and the transition function  $\delta : Q \times \Sigma \rightarrow P(\Sigma)$  where  $\delta(q_0, 0) = \{q_0, q_1\}$ ,  $\delta(q_0, 1) = \{q_0, q_2\}$ , and  $\delta(q, \sigma) = \emptyset$  for  $q \in \{q_1, q_2\}$  and all  $\sigma \in \Sigma$ . Construct a DFSM  $D$  such that  $L(N) = L(D)$ . *Hint:* Use the Subset Construction, cf. Section 2.2 in the lecture notes.

**Problem 7.** Let the DFSM  $M = (Q, \Sigma, \delta, q_0, F)$  be given by  $Q = \{q_0, q_1, q_2\}$ ,  $\Sigma = \{0, 1\}$ ,  $F = \{q_1, q_2\}$  and the following transition function  $\delta : Q \times \Sigma \rightarrow Q$ :



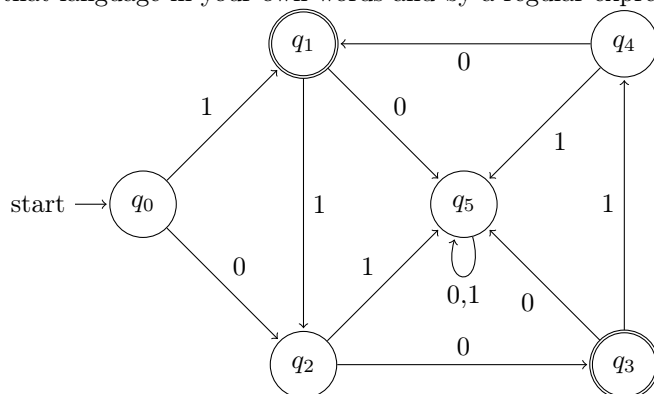
Construct a minimal DFSM  $D$  such that  $L(M) = L(D)$  using Algorithm MINIMIZE. (cf. Section 2.3 *Minimization of Finite State Machines*)

**Problem 8.** Construct a nondeterministic finite state machine for:

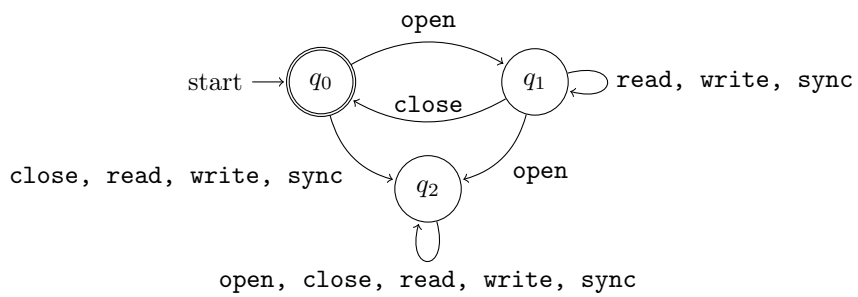
1. the language  $L_1$  of all strings over  $\{0, 1\}$  that contain 001 as a substring.
2. the language  $L_2$  of all strings over  $\{0, 1\}$  that contain the letters 0, 0, 1 in exactly that order. (Note that before, in between and after these three letters any number of other letters may occur).

Your two machines must not use more than 4 states. Moreover, they should only differ in their transition functions. Draw their transition graphs.

**Problem 9.** What language is accepted by the DFSM depicted below? Describe that language in your own words and by a regular expression.



**Problem 10.** What is the language  $L(M)$  of the following deterministic finite-state machine  $M$



over the alphabet  $\Sigma = \{\text{open, close, read, write, sync}\}$ ? Give a regular expression  $r$  such that  $L(M) = L(r)$ .