Formal Methods in Software Development Assignment 1 (October 30)

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The result is to be submitted by the deadline stated above *via the Moodle interface* of the course as a .zip or .tgz file which contains

- 1. a PDF file with
 - a cover page with the course title, your name, Matrikelnummer, and email address,
 - a section for each part of the exercise with the requested deliverables and optionally any explanations or comments you would like to make;
- 2. the RISCAL specification (.txt) file(s) used in the exercise.

Email submissions are not accepted.

Assignment 1: Validating and Checking Program Specifications

We consider the following two problems:

- 1. Given an array a and a positive integer n, find the minimum of the first n elements of a, i.e., that element m that occurs at some of the first n positions of a and that is less than or equal all elements at these positions.
- 2. Given an array a and a positive integer n, find an index of the minimum of the first n elements of a, i.e., a non-negative integer p less than n such that the element of a at p is that minimum.

In the RISCAL specification file minimum.txt you find two procedures minimumElement and minimumIndex that are supposed to solve these problems, respectively (but the procedures may contain bugs). The specification is based on two integer types int and elem that bound the domain of possible array indices respectively elements by constants N and M respectively.

For *each* of the procedures perform the following tasks (the definitions already given in the specification file must *not* be modified unless explicitly noted):

- (a) Formalize the procedure's precondition and postcondition as predicates.
 - Here do not use the arithmetic quantifier min but only the predicate logic quantifiers \forall and \exists (translate above specification from natural language to logic). Hint: a formula $(\forall v:T \text{ with } F. G)$ is equivalent to $(\forall v:T. F \Rightarrow G)$ and a formula $(\exists v:T \text{ with } F. G)$ is equivalent to $(\exists v:T. F \land G)$; you may use either notation.
- (b) Use the precondition and postcondition to implicitly define a function and check whether the computed results are as desired.
- (c) Formulate a theorem that states that some input satisfies the precondition and check this theorem.
- (d) Formulate a theorem that states that not every input satisfies the precondition and check this theorem.
- (e) Formulate a theorem that states that, for every input that satisfies the precondition, there exists some output that satisfies the postcondition, and check that theorem.
- (f) Formulate a theorem that states that, for every input that satisfies the precondition, not every output satisfies the postcondition, and check that theorem.
- (g) Formulate a theorem that states that, for every input that satisfies the precondition, the output is uniquely defined by the postcondition, and check that theorem.
- (h) Annotate the procedure with preconditions and postconditions and check the correctness of the procedure for every possible array *a* and length *n*; if a condition is a conjunction, it is recommended to use multiple annotation clauses.

Perform all checks with some small $N \ge 3$ and $M \ge 1$.

Perform the function execution (b) with translation option "Nondeterminism" selected; for all other checks you may unselect this option.

If a theorem is not valid, give an explanation of why the theorem is not valid and whether this indicates an error in your specification or not. For this purpose, select the visualization option "Tree" and investigate the evaluation of the theorem (if the tree layout is unsatisfactory, choose larger visualization width/height and/or smaller values of N and M).

If the execution of a procedure gives an error, give an explanation of why this is the case and whether this indicates an error in the procedure or not. To investigate the error, use the procedure main to choose the input exhibiting the error. Select the visualization option "Trace" and investigate the corresponding execution (if a postcondition fails, comment out the postcondition before starting the execution, otherwise no trace is generated); for this, click on the node denoting the procedure call to see the trace of the procedure execution. If the error indicates a bug in the procedure, fix this bug.

The deliverables for this exercise consists of the following items:

- 1. a nicely formatted copy of the extended specification (included as text, not as screenshots);
- 2. for each check, a selection of the output of reasonable size (included as text, not as screenshots);
- 3. if a check gives an error, a screenshot of the visualization exhibiting that error, an explanation of the error, and a justified statement that describes whether this indicates an error in your specifications or not;
- 4. if you fixed a bug in a procedure, a clear indication and explanation of that fix.