

- Freely available since 1991.
- Symposium series since 1995 (28th symposium "Spin 2022").
- ACM System Software Award in 2001.

Spin resources:

- Web site: http://spinroot.com.
- Survey paper: Holzmann "The Model Checker Spin", 1997.
- Book: Holzmann "The Spin Model Checker Primer and Reference Manual", 2004.

Goal: verification of (concurrent/distributed) software models.



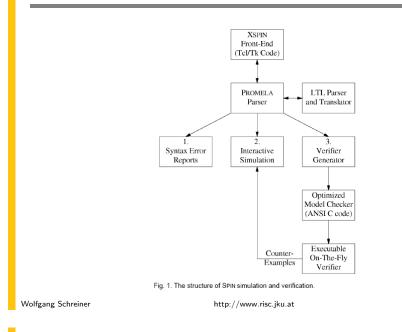
- Explicit representation of automaton states.
- There exist various other approaches (discussed later).
- On-the-fly model checking.
 - Reachable states of S_A are only expended on demand.
 - Partial order reduction to keep state space manageable.
- LTL model checking.
 - Property P to be checked described in PLTL.
 - Propositional linear temporal logic.
 - Description converted into property automaton P_A .
 - Automaton accepts only system runs that do not satisfy the property.

Model checking based on automata theory.

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The Spin System Architecture

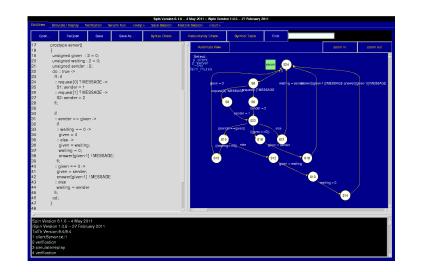




The Spin User Interface



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Features of Spin



- System description in Promela.
 - Promela = Process Meta-Language.
 - Spin = Simple Promela Interpreter.
 - Express coordination and synchronization aspects of a real system.
 - Actual computation can be e.g. handled by embedded C code.

Simulation mode.

- Investigate individual system behaviors.
- Inspect system state.
- Graphical interface ispin for visualization.

Verification mode.

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- Verify properties shared by all possible system behaviors.
- Properties specified in PLTL and translated to "never claims".
 - Promela description of automaton for negation of the property.
- Generated counter examples may be investigated in simulation mode.

Verification and simulation are tightly integrated in Spin.

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The Client/Server System in Promela



<pre>/* definition of a constant MESSAGE */ mtype = { MESSAGE };</pre>	<pre>/* the client process type */ proctype client(byte id) {</pre>
<pre>/* two arrays of channels of size 2, each channel has a buffer size 1 */ chan request[2] = [1] of { mtype }; chan answer [2] = [1] of { mtype };</pre>	<pre>do :: true -> request[id-1] ! MESSAGE; W: answer[id-1] ? MESSAGE; C: skip; // the critical region request[id-1] ! MESSAGE</pre>
<pre>/* the system of three processes */</pre>	od;
init	}
{	
<pre>run client(1);</pre>	
<pre>run client(2);</pre>	
<pre>run server();</pre>	
}	

/* the mutual exclusion property */ ltl mutex { []!(client[1]@C && client[2]@C)}

The Client/Server System in Promela



/* the server process type */	<pre>/* answering the message */</pre>
proctype server()	if
{	:: sender == given ->
<pre>/* three variables of two bit each */</pre>	if
unsigned given : 2 = 0;	:: waiting == 0 ->
unsigned waiting : 2 = 0;	given = 0
unsigned sender : 2;	:: else ->
	given = waiting;
do :: true ->	<pre>waiting = 0;</pre>
	answer[given-1] ! MESSAGE
<pre>/* receiving the message */</pre>	fi;
R: if	:: given == 0 ->
:: request[0] ? MESSAGE ->	given = sender;
S1: sender = 1	answer[given-1] ! MESSAGE
<pre>:: request[1] ? MESSAGE -></pre>	:: else
S2: sender = 2	waiting = sender
fi;	fi;
	od;
	}

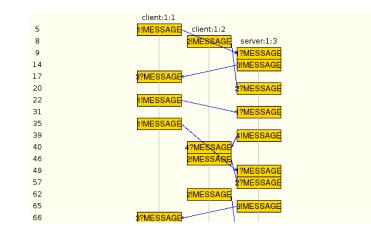
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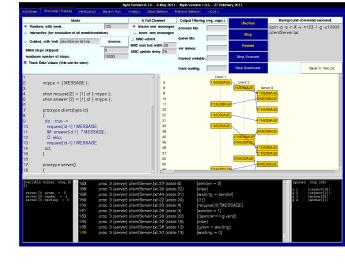
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Simulating the System Execution in Spin





The Spin Simulation View



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The Spin Verification View

Safety	Storage Mode	Search Mode				
♦ safety	exhaustive	+ depth-first search		Rem	ove	
+ invalid endstates (deadlook)	+ minimized automata (slow)	+ partial order reduction		Advanced: F	Parameters	
+ assertion violations	+ collapse compression	+ bounded context switching		Physical Memory Available (in Mbyles):	1024	expl
+ xr/xs assertions	♦ hash-compact ♦ bitstale/supertrace	with bound: 0		,	1	
Liveness	Never Claims	+ llerative search for short trail		Estimated State Space Size (states x 10 ^ 3):	1000	expl
on progress cycles	Ido not use a never claim or III property	breadth-first search		-		
 acceptance cycles 	+ use claim	+ partial order reduction	Show	Maximum Search Depth (steps):	10000	expl
enforce weak fairness constraint	olaim name (opt):	report unreachable code	Error Trapping	Nr of hash-functions in Bitstate mode:	3	expl
		Save Result in pan.out	Options			
				Size for Minimized Automation	100	expl
				Edra Veriller Generation Options:		expl
				Edra Complie Time Directives:	02	expl
	Run Stop			Edra Run-Time Options:		expl
3 chan request[2] = [' 4 chan answer[2] = [' 5 chan answer[2] = [' 6 proctype client(byte 7 P (accuration) 8 doi:::tue-> 10 ::maswer[d-1] 11 W: answer[d-1] 12 C; skip; 13 request[d-1] 14 od; 15 } 16 } 17 proctype server()] of { mtype }; id) SSAGE; MESSAGE;	Jpan +n 10000 - a Pid: 16183 warning: forp o. r (rever claims ger (Spin Version 6.1. + Parie Full atatespace s secont asserti asserti	eduction to be erated from L 04 May 201 I Order Redu arch for: aim +1 n violations +1 nce cycles		างสก่อกร	
18 { 19 unsigned given : 2 20 unsigned waiting : 21 unsigned sender :	2 = 0;	State-vector 48 by 157 states, sto 68 states, ma	red	ched 137, errors: 0		



Specifying a System Property in Spin



The easiest way to specify an LTL property is to specify it inline. The formula is specified globally (i.e., outside all proctype or init declarations) with the following syntax:

ltl [name] '{' formula '}'

... The names of operators can either be abbreviated with the symbols shown above, or spelled out in full (as always, eventually, until, implies, and equivalent. The alternative operators weakuntil, stronguntil, and release (for the V operator, see above), are also supported. This means that the following two are equivalent:

ltl p1 { []<> p }
ltl p2 { always eventually p }
ltl p3 { eventually (a > b) implies len(q) == 0 }

There is just one restriction: you cannot use the predefined operators empty, nempty, full, nfull in inline ltl formula...

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Spin Atomic Predicates



(a+b > c) (len(q) < 5) (process@Label) (process[pid]@Label)

- PROMELA conditions with references to *global* system variables.
 - C-like boolean expressions.
 - len(q): the number of messages in channel q.
 - process@Label: true if the execution of the process with process type process is in the state marked by Label.
 - process[pid]@Label: true if the execution of the process with type process and process identifier pid is in the state marked by Label.
 - Process init receives identifier 0.
 - Processes instantiated with run receive identifiers 1, 2,

Atomic predicates can describe arbitrary state conditions.

Spin LTL



Grammar:

ltl ::= opd | (ltl) | ltl binop ltl | unop ltl

Operands (opd):

true, false, user-defined names starting with a lower-case letter, or embedded expressions inside curly braces, e.g.,: { a+b>n }.

Unary Operators (unop):

- [] (the temporal operator always)
- <>(the temporal operator eventually)
- ! (the boolean operator for negation)

Binary Operators (binop):

- U (the temporal operator strong until)
- W (the temporal operator weak until)
- V (the dual of U): (p V q) means !(!p U !q))
- && (the boolean operator for logical and)
- $\left| \cdot \right|$ (the boolean operator for logical or)
- $/ \$ (alternative form of &&)
- $\backslash/$ (alternative form of ||)
- -> (the boolean operator for logical implication)
- <-> (the boolean operator for logical equivalence)

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The Spin Verification Options

Verification mode

- Safety: predefined safety properties.
- Liveness: predefined liveness properties.
- Use Claim: user-defined (LTL) properties.
- Storage mode

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- **Exhaustive:** full error search.
 - May require (too) much memory.
- Hash-compact and bitstate/supertrace: probabilistic search.
 - Less memory consuming but not guaranteed to find all errors.
 - Number of reported hash collisions should not be too high.
- Advanced Parameters
 - Physical Memory Size: increase, if checker runs out of memory.
 - Maximum Search Depth: reduce to find shorter counterexamples.
- By default, select "use claim" and "exhaustive".

The Spin Verification Output



(Spin Version 6.1.0 -- 4 May 2011) + Partial Order Reduction Full statespace search for: never claim + (mutex) assertion violations + (if within scope of claim) acceptance cycles + (fairness disabled) invalid end states - (disabled by never claim) State-vector 48 byte, depth reached 137, errors: 0 157 states, stored 68 states, matched 225 transitions (= stored+matched) 0 atomic steps 0 (resolved) hash conflicts: Stats on memory usage (in Megabytes): . . . pan: elapsed time 0 seconds No errors found -- did you verify all claims? Wolfgang Schreiner http://www.risc.jku.at 17/47 More Promela Features

Embedded C code.

```
/* declaration is added locally to proctype main */
c_state "float f" "Local main"
active proctype main()
{
    c_code { Pmain->f = 0; }
    do
        :: c_expr { Pmain->f <= 300 };
        c_code { Pmain->f = 1.5 * Pmain->f ; };
        c_code { printf("%4.0f\n", Pmain->f); };
    od;
}
```

Can embed computational aspects into a Promela model (only works in verification mode where a C program is generated from the model).

More Promela Features



Active processes, inline definitions, atomic statements, output.

```
mtype = \{ P, C, N \}
       mtype turn = P;
       inline request(x, y) { atomic { x == y \rightarrow x = N } }
       inline release(x, y) { atomic { x = y } }
       #define FORMAT "Output: %c\n"
       active proctype producer()
       ſ
         do
         :: request(turn, P) -> printf(FORMAT, 'P'); release(turn, C);
         od
       }
       active proctype consumer()
       Ł
         do
         :: request(turn, C) -> printf(FORMAT, 'C'); release(turn, P);
         od
       }
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```



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1. The Model Checker Spin

2. Automatic Model Checking

The Basic Approach



Translation of the original problem to a problem in automata theory.

- Original problem: $S \models P$.
 - $S = \langle I, R \rangle$, PLTL formula *P*.
 - Does property *P* hold for every run of system *S*?
- Construct system automaton S_A with language $\mathcal{L}(S_A)$.
 - A language is a set of infinite words.
 - Each such word describes a system run.
 - $\mathcal{L}(S_A)$ describes the set of runs of S.
- Construct property automaton P_A with language $\mathcal{L}(P_A)$.
 - $\mathcal{L}(P_A)$ describes the set of runs satisfying P.
- Equivalent Problem: $\mathcal{L}(S_A) \subseteq \mathcal{L}(P_A)$.
 - The language of S_A must be contained in the language of P_A .

There exists an efficient algorithm to solve this problem.

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Runs and Languages



- An infinite run $r = s_0 \xrightarrow{l_0} s_1 \xrightarrow{l_1} s_2 \xrightarrow{l_2} \dots$ of automaton A: • $s_0 \in I$ and $R(I_i, s_i, s_{i+1})$ for all $i \in \mathbb{N}$.
 - Run r is said to read the infinite word $w(r) := \langle l_0, l_1, l_2, \ldots \rangle$.
- $A = \langle I, R, F \rangle$ accepts an infinite run r:
 - Some state $s \in F$ occurs infinitely often in r.
 - This notion of acceptance is also called Büchi acceptance.
- The language $\mathcal{L}(A)$ of automaton A:
 - $\mathcal{L}(A) := \{ w(r) : A \text{ accepts } r \}.$
 - The set of words which are read by the runs accepted by A.

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- Example: $\mathcal{L}(A) = (a^*bb^*a)^*a^\omega + (a^*bb^*a)^\omega = (b^*a)^\omega$
 - $w^i = ww \dots w$ (*i* occurrences of *w*).
 - $w^* = \{w^i : i \in \mathbb{N}\} = \{\langle \rangle, w, ww, www, \ldots\}.$
 - $w^{\omega} = wwww...$ (infinitely often).
 - An infinite repetition of an arbitrary number of *b* followed by *a*.

Figure 9.1		
A finite automaton.		
11 mile untomatom		

Edmund Clarke: "Model Checking", 1999. 23/47

Finite State Automata



A (variant of a) labeled transition system in a finite state space.

- Take finite sets *State* and *Label*.
 - The state space *State*.
 - The alphabet *Label*.
- A (finite state) automaton $A = \langle I, R, F \rangle$ over State and Label:
 - A set of initial states $I \subset State$.
 - A labeled transition relation $R \subset Label \times State \times State$.
 - A set of final states $F \subseteq State$.
 - Büchi automata: *F* is called the set of accepting states.

We will only consider infinite runs of Büchi automata.

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A Finite State System as an Automaton

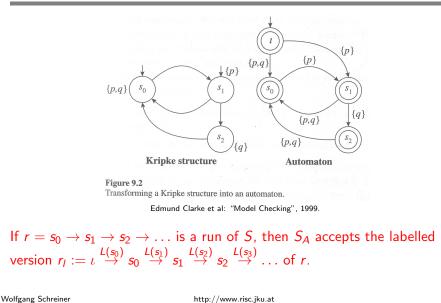


- The automaton $S_A = \langle I, R, F \rangle$ for a finite state system $S = \langle I_S, R_S \rangle$: • State := State $\varsigma \cup \{\iota\}$.
 - The state space *States* of *S* is finite; additional state ι ("iota").
 - Label := $\mathbb{P}(AP)$.
 - Finite set *AP* of atomic propositions.
 - All PLTL formulas are built from this set only.
 - Powerset $\mathbb{P}(S) := \{s : s \subset S\}.$
 - Every element of *Label* is thus a set of atomic propositions.
 - $I := \{\iota\}.$
 - Single initial state ι .
 - $\blacksquare R(I, s, s') : \Leftrightarrow I = L(s') \land (R_{S}(s, s') \lor (s = \iota \land I_{S}(s'))).$
 - $L(s) := \{ p \in AP : s \models p \}.$
 - Each transition is labeled by the set of atomic propositions satisfied by the successor state.
 - F := State.
 - Every state is accepting.

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A Finite State System as an Automaton



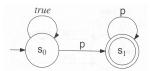


Further Examples



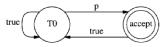
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Example: $\Diamond \Box p$.



Gerard Holzmann: "The Spin Model Checker", 2004.

Example: $\Box \Diamond p$.



Gerard Holzmann: "The Model Checker Spin", 1997.

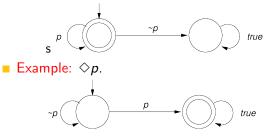
Arbitrary PLTL formulas can be converted to automata (we omit the details).

A System Property as an Automaton



Also an PLTL formula can be translated to a finite state automaton.

- We need the automaton P_A for a PLTL property P.
 - Requirement: $r \models P \Leftrightarrow P_A$ accepts r_I .
 - A run satisfies property *P* if and only if automaton *A_P* accepts the labeled version of the run.
- **Example:** $\Box p$.



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System Properties

- **State equivalence**: L(s) = L(t).
 - Both states have the same labels.
 - Both states satisfy the same atomic propositions in *AP*.
- **Run equivalence**: $w(r_l) = w(r'_l)$.
 - Both runs have the same sequences of labels.
 - Both runs satisfy the same PLTL formulas built over AP.
- Indistinguishability: $w(r_l) = w(r'_l) \Rightarrow (r \models P \Leftrightarrow r' \models P)$
 - PLTL formula P cannot distinguish between runs r and r' whose labeled versions read the same words.
- Consequence: $S \models P \Leftrightarrow \mathcal{L}(S_A) \subseteq \mathcal{L}(P_A)$.
 - If every run of S satisfies P, then every word $w(r_l)$ in $\mathcal{L}(S_A)$ equals some word $w(r'_l)$ in $\mathcal{L}(P_A)$, and vice versa.

The Next Steps



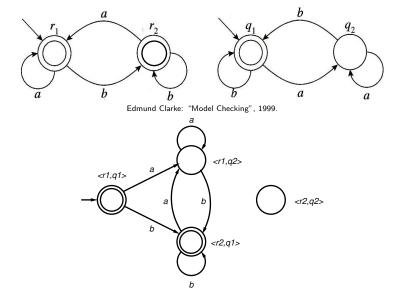
- Problem: L(S_A) ⊆ L(P_A)
 Equivalent to: L(S_A) ∩ L(P_A) = Ø.
 Complement I := {w : w ∉ L}.
 Equivalent to: L(S_A) ∩ L((¬P)_A) = Ø.
 L(P_A) = L((¬P)_A).
 Equivalent Problem: L(S_A) ∩ L((¬P)_A) = Ø.
 We will introduce the synchronized product automaton A ⊗ B.
 A transition of A ⊗ B represents a simultaneous transition of A and B.
 Property: L(A) ∩ L(B) = L(A ⊗ B).
 Final Problem: L(S_A ⊗ (¬P)_A) = Ø.
 We have to check whether the language of this automaton is empty.
 We have to look for a word w accepted by this automaton.
 - If no such w exists, then $S \models P$.
 - If such a $w = w(r_l)$ exists, then r is a counterexample, i.e. a run of S such that $r \not\models P$.

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Synchronized Product of Two Automata





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Synchronized Product of Two Automata



Given two finite automata $A = \langle I_A, R_A, State_A \rangle$ and $B = \langle I_B, R_B, F_B \rangle$. Synchronized product $A \otimes B = \langle I, R, F \rangle$.

- State := State_A × State_B.
- Label := $Label_A = Label_B$.
- $I := I_A \times I_B.$
- $\blacksquare R(I, \langle s_A, s_B \rangle, \langle s'_A, s'_B \rangle) :\Leftrightarrow R_A(I, s_A, s'_A) \land R_B(I, s_B, s'_B).$
- $F := State_A \times F_B$.

Special case where all states of automaton A are accepting.

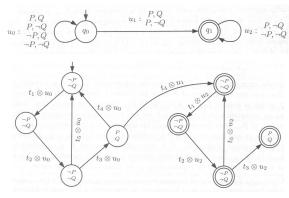
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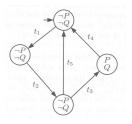
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Example

Check whether $S \models \Box(P \Rightarrow \bigcirc \diamondsuit Q)$.





B. Berard et al: "Systems and Software Verification", 2001.

The product automaton accepts a run, thus the property does not hold (shown *S* has no ι but t_i labeled with properties of predecessor state). Wolfgang Schreiner

Checking Emptiness



How to check whether $\mathcal{L}(A)$ is non-empty?

- If $\mathcal{L}(A)$ is non-empty, A accepts some run r.
 - r represents a counterexample for the property to be checked.
- Since r is accepted, it contains infinitely many occurrences of some accepting state s.
 - $r = \iota \rightarrow \ldots \rightarrow s \rightarrow \ldots \rightarrow s \rightarrow \ldots \rightarrow s \rightarrow \ldots$
- Since the state space is finite, r must contain a cycle $s \rightarrow \ldots \rightarrow s$.
 - Finite prefix $\iota \to \ldots \to s$.
 - Infinite repetition of cycle $s \rightarrow \ldots \rightarrow s$.
- We have to search for such an acceptance cycle.
 - An accepting state *s* that is reachable from itself.

The search for an acceptance cycle in the reachability graph is the core problem of PLTL model checking; it can be solved by *depth-first search*.

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Searching for a State



Algorithm to check violation of assertion f (i.e., $\Box f$ with state formula f).

global	function search(s)
StateSpace $V := \{\}$	$V := V \cup \{s\}$
Stack $D := \langle \rangle$	if $s \not\models f$ then
	print D
proc main()	return true
<pre>// r becomes true, iff</pre>	end
<pre>// counterexample run is found</pre>	for $\langle I, s, s' \rangle \in R$ do
$push(D, \iota)$	if $s' \not\in V$
$r := search(\iota)$	push(D, s')
pop(D)	r := search(s')
end	pop(D)
	if r then return true end
	end
	end
	return false
	end

Stack *D* can be used to print counterexample run.

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Visit all states of the reachability graph of an automaton $\langle \{\iota\}, R, F \rangle$.

global <i>StateSpace</i> V := {}	$\begin{array}{l} proc \ visit(s) \\ \mathcal{V} := \mathcal{V} \cup \{s\} \end{array}$
Stack $D := \langle \rangle$	for $\langle I, s, s' \rangle \in R$ do
	if $s' \notin V$
proc main()	push(D, s')
$push(D, \iota)$	visit(s')
$visit(\iota)$	pop(D)
pop(D)	end
end	end
	end

State space V holds all states visited so far; stack D holds path from initial state to currently visited state.

```
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```

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Searching for an Acceptance Cycle



Algorithm to check whether a general temporal formula is violated.

global	proc main()
StateSpace V := {}	$push(D, \iota); r := search(\iota); pop(D)$
Stack $D := \langle \rangle$	end
Stack $C := \langle \rangle$	
	boolean search(s)
function searchCycle(s)	$V := V \cup \{s\}$
for $\langle I, s, s' \rangle \in R$ do	for $\langle I, s, s' \rangle \in R$ do
if $has(D, s')$ then	if $s' \notin V$
print D; print C; print s'	push(D, s')
return true	r := search(s')
else if $\neg has(C, s')$ then	pop(D)
push(C, s');	if r then return true end
r := searchCycle(s')	end
pop(C);	end
if r then return true end	if $s \in F$ then
end	r := searchCycle(s)
end	if r then return true end
return false	end
end	return false
	end

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Depth-First Search for Acceptance Cycle



- At each call of search(s),
 - s is a reachable state,
 - D describes a path from ι to s.
- search calls searchCycle(s)
 - on a reachable accepting state s
 - in order to find a cycle from s to itself.
- At each call of searchCycle(s),
 - **s** is a state reachable from a reachable accepting state s_a ,
 - D describes a path from ι to s_a ,
 - $D \rightarrow C$ describes a path from ι to s (via s_a).
- \blacksquare Thus we have found an accepting cycle $D \to C \to s',$ if
 - there is a transition $s \stackrel{l}{\rightarrow} s'$,
 - such that s' is contained in D.

If the algorithm returns "true", there exists a violating run; the converse follows from the exhaustiveness of the search.

Complexity of the Search



The complexity of checking $S \models P$ is as follows.

- Let |P| denote the number of subformulas of P.
- $|State_{(\neg P)_A}| = O(2^{|P|}).$
- $|State_{A\otimes B}| = |State_A| \cdot |State_B|.$
- $|State_{S_A \otimes (\neg P)_A}| = O(|State_{S_A}| \cdot 2^{|P|})$
- The time complexity of *search* is linear in the size of *State*.
 - Actually, in the number of reachable states (typically much smaller).
 - Only true for the improved variant where the *c* bits are not reset.
 - Then every state is visited by *searchCycle* at most once.

PLTL model checking is linear in the number of reachable states but exponential in the size of the formula.

Implementing the Search



The state space V,

- is implemented by a hash table for efficiently checking $s' \notin V$.
- Rather than using explicit stacks D and C,
 - each state node has two bits *d* and *c*,
 - d is set to denote that the state is in stack D,
 - *c* is set to denote that the state is in stack *C*.
- The counterexample is printed,
 - by searching, starting with *ι*, the unique sequence of reachable nodes where *d* is set until the accepting node *s_a* is found, and
 - by searching, starting with a successor of s_a, the unique sequence of reachable nodes where c is set until the cycle is detected.
- Furthermore, it is not necessary to reset the *c* bits, because
 - search first explores all states reachable by an accepting state s before trying to find a cycle from s; from this, one can show that
 - called with first accepting node s_a reachable from itself, searchCycle needs not revisit nodes with c bits set in previous searches.
 - With this improvement, every state is only visited once.

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The Overall Process

Basic PLTL model checking for deciding $S \models P$.

- Convert system S to automaton S_A .
 - Atomic propositions of PLTL formula are evaluated on each state.
- Convert negation of PLTL formula P to automaton $(\neg P)_A$.
 - How to do so, we have not yet described.
- Construct synchronized product automaton $S_A \otimes (\neg P)_A$.
 - After that, formula labels are not needed any more.
- Find acceptance cycle in reachability-graph of product automaton.
 - A purely graph-theoretical problem that can be efficiently solved.
 - Time complexity is linear in the size of the state space of the system but exponential in the size of the formula to be checked.
 - Weak scheduling fairness with k components: runtime is increased by factor k + 2 (worst-case, "in practice just factor 2" [Holzmann]).

The basic approach immediately leads to *state space explosion*; further improvements are needed to make it practical.

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For checking $\mathcal{L}(S_A \otimes (\neg P)_A) = \emptyset$, it is not necessary to construct the states of S_A in advance.

- Only the property automaton $(\neg P)_A$ is constructed in advance.
 - This automaton has comparatively small state space.
- **The system automaton** S_A is constructed on the fly.
 - Construction is guided by $(\neg P)_A$ while computing $S_A \otimes (\neg P)_A$.
 - Only that part of the reachability graph of S_A is expanded that is consistent with $(\neg P)_A$ (i.e. can lead to a counterexample run).
- **Typically only a part of the state space of** S_A is investigated.
 - A smaller part, if a counterexample run is detected early.
 - A larger part, if no counterexample run is detected.

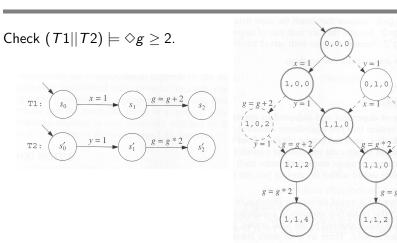
Unreachable system states and system states that are not along possible counterexample runs are never constructed.

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Example



Gerard Holzmann: "The Spin Model Checker", 1999.

For checking $\Diamond g \geq 2$, it suffices to check only one ordering of the independent transitions x = 1 and y = 1 (not true for checking $\Box x \ge y$). Wolfgang Schreiner http://www.risc.jku.at 43/47

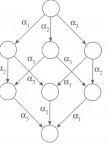
Partial Order Reduction



Core problem of model checking: state space explosion.

- Take asynchronous composition $S_0||S_1|| \dots ||S_{k-1}|$.
 - Take state s where one transition of each component is enabled.
 - Assume that the transition of one component does not disable the transitions of the other components and that no other transition becomes enabled before all the transitions have been performed.
 - Take state s' after execution of all the transitions
 - There are k! paths leading from s to s'.
 - **There are 2^k states involved in the transitions.**

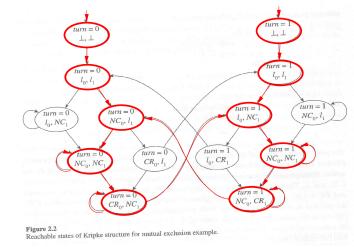
Sometimes it suffices to consider a single path with k + 1 states.



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Edmund Clarke: "Model Checking", 1999. http://www.risc.jku.at

Example



Edmund Clarke et al: "Model Checking", 1999.

System after partial order reduction.

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Other Optimizations



Statement merging.

- Special case of partial order reduction where a sequence of transitions of same component is combined to a single transition.
- State compression.
 - Collapse compression: each state holds pointers to component states; thus component states can be shared among many system states.
 - Minimized automaton representation: represent state set V not by hash table but by finite state automaton that accepts a state (sequence of bits) s if and only if s ∈ V.
 - Hash compact: store in the hash table a hash value of the state (computed by a different hash function). Probabilistic approach: fails if two states are mapped to the same hash value.
 - Bitstate hashing: represent V by a bit table whose size is much larger than the expected number of states; each state is then only represented by a single bit. Probabilistic approach: fails if two states are hashed to the same position in the table.

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Other Approaches to Model Checking



- Counter-Example Guided Abstraction Refinement (e.g. BLAST).
 - Core: model abstraction.
 - A finite set of predicates is chosen and an abstract model of the system is constructed as a finite automaton whose states represent truth assignments of the chosen predicates.
 - The abstract model is checked for the desired property.
 - If the abstract model is error-free, the system is correct; otherwise an abstract counterexample is produced.
 - It is checked whether the abstract counterexample corresponds to a real counterexample; if yes, the system is not correct.
 - If not, the chosen set of predicates contains too little information to verify or falsify the program; new predicates are added to the set. Then the process is repeated.
 - **Core problem**: how to refine the abstraction.
 - Automated theorem provers are applied here.
- Various model checkers for software verification use this approach.



There are fundamentally different approaches to model checking than the automata-based one implemented in Spin.

- Symbolic Model Checking (e.g. SMV, NuSMV).
 - Core: binary decision diagrams (BDDs).
 - Data structures to represent boolean functions.
 - Can be used to describe state sets and transition relations.
 - The set of states satisfying a CTL formula P is computed as the BDD representation of a fixpoint of a function (predicate transformer) F_P.
 - If all initial system states are in this set, P is a system property.
 - BDD packages for efficiently performing the required operations.
- Bounded Model Checking (e.g. NuSMV2).
 - Core: propositional satisfiability.
 - Is there a truth assignment that makes propositional formula true?
 - There is a counterexample of length at most k to a LTL formula P, if and only if a particular propositional formula $F_{k,P}$ is satisfiable.

Problem: find suitable bound k that makes method complete.

SAT solvers for efficiently deciding propositional satisfiability.

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