Unranked Anti-Unification and Its Application in Software Code Clone Detection

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What Are Code Clones

- Similar pieces of software code.
- Obtained by reusing code fragments.
- Quite typical practice.



Why Should Clones Be Detected?

- In general, they are harmful:
 - Additional maintenance effort.
 - Additional work for enhancing and adapting.
 - Inconsistencies presenting fault.

Why Should Clones Be Detected?

 Extraction of similar code fragments may be required in the tasks of

- program understanding
- code quality analysis
- aspect mining
- plagiarism detection
- copyright infringement investigation
- software evolution analysis
- code compaction
- bug detection



Classification

Roy, Cordy and Koschke (2009) distinguish four types of clones:

- Type 1: Identical code fragments except for variations in whitespace, layout and comments.
- Type 2: Syntactically identical fragments except for variations in identifiers, literals, types, whitespace, layout and comments.
- Type 3: Copied fragments with further modifications such as changed, added or removed statements, in addition to variations in identifiers, literals, types, whitespace, layout and comments.
- Type 4: Two or more code fragments that perform the same computation but are implemented by different syntactic variants.
- 1-3: Syntactic clones.



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Examples of Syntactic Clone Types

Type 1: Identical code fragments except for variations in whitespace, layout and comments.



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Type 2: Syntactically identical fragments except for variations in identifiers, literals, types, whitespace, layout and comments.

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Generic Clone Detection Process

From Roy, Cordy, and Koschke (2009):

- 1. Preprocessing: Remove uninteresting code, determine source and comparison units/granularities.
- 2. Transformation: Obtain an intermediate representation of the preprocessed code.
- 3. Detection: Find similar source units in the transformed code.
- 4. Formatting: Clone locations of the transformed code are mapped back to the original code.
- 5. Filtering: Clone extraction, visualization, and manual analysis to filter out false positives.

Clone Detection Techniques

From Roy, Cordy, and Koschke (2009):

- 1. Text-based: Little transformation, mostly raw source code in the detection process.
- 2. Token-based: Transforming the source code into a sequence of lexical "tokens". The sequence is then scanned for duplicated subsequences of tokens.
- 3. Tree-based: Transforming the source code into trees (parse trees, ASTs, ...) which can then be processed using either tree comparison or structural metrics to find clones.
- 4. Metrics-based: Gathering a number of metrics for code fragments and then compare metrics vectors rather than code or trees directly.
- 5. Graph-based: Find isomorphic subgraphs in PDGs.
- 6. Hybrid approaches.



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Our Idea

- 1. Aiming at high precision for clones of type 3.
- 2. Tree-based approach (possibly combined with text- and metrics-based)
- 3. In the clone detection step, use anti-unification.



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- 4. Existing anti-unification based tools:
 - CloneDigger (Bulychev et al. 2009).
 - Wrangler (Li and Thompson, 2010).
 - ► HaRe (Brown and Thompson, 2010).

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 - ► HaRe (Brown and Thompson, 2010).
- 5. We propose using unranked anti-unification instead of the standard one.



Unranked alphabet: The arity of function symbols is not fixed.

- Variables: Term variables x, y, z, ... and hedge variables X, Y, Z, ...
 - Terms: A term variable or a compound term of the form $f(s_1, \ldots, s_n)$.
 - Hedges: A sequence s_1, \ldots, s_n where each s_i is either a hedge variable or a term.

Substitutions

Substitution: a mapping

- from term variables to terms,
- from hedge variables to hedges,

which is identity almost everywhere.



Terms and Substitutions

Example

 $f(g(X), f(Y), g(a, y)) \qquad \{X \mapsto (), Y \mapsto (g(a), y), y \mapsto f(a)\}$





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Hedge Generalization

A hedge \tilde{s} is a generalization (anti-instance) of the hedges \tilde{s}_1 and \tilde{s}_2 if

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- \tilde{s} is more general than \tilde{s}_1 ($\tilde{s} \leq \tilde{s}_1$) and
- \tilde{s} is more general than \tilde{s}_2 ($\tilde{s} \leq \tilde{s}_2$),

i.e., if there exist σ_1 and σ_2 such that

•
$$\tilde{s}\sigma_1 = \tilde{s}_1$$
 and

•
$$\tilde{s}\sigma_2 = \tilde{s}_2$$
.

A hedge \tilde{s} is a least general generalization (lgg) of the hedges \tilde{s}_1 and \tilde{s}_2 if

- \tilde{s} is a generalization of \tilde{s}_1 and \tilde{s}_2 and
- no generalization of \tilde{s}_1 and \tilde{s}_2 is strictly less general than \tilde{s} .



A minimal complete set of generalizations of \tilde{s}_1 and \tilde{s}_2 is a set \mathcal{G} of hedges that satisfies the properties:

Soundness: Each $\tilde{q} \in G$ is a generalization of both \tilde{s}_1 and \tilde{s}_2 . Completeness: For each generalization \tilde{s} of \tilde{s}_1 and \tilde{s}_2 , there exists $\tilde{q} \in G$ such that $\tilde{s} \preceq \tilde{q}$. Minimality: For each $\tilde{q}_1, \tilde{q}_2 \in G$, if $\tilde{q}_1 \prec \tilde{q}_2$ then $\tilde{q}_1 = \tilde{q}_2$.



The Anti-Unification Problem

Given: Two hedges \tilde{s}_1 and \tilde{s}_2 . Find: The minimal complete set of generalizations of \tilde{s}_1 and \tilde{s}_2 .



Example

What is the minimal complete set of generalizations of g(f(a), f(a)) and g(f(a), f)?



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$$\{X \mapsto a, Y \mapsto \epsilon\} \qquad \{X \mapsto \epsilon, Y \mapsto a\}$$
$$g(f(a), f(a)) \qquad g(f(a), f)$$



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- Emphasis on keeping the common structure, rather than on uniform generalization of distinct parts.
- Avoiding consecutive hedge variables in the generalization.



More specifically:

• Given two hedges $f_1(\tilde{s}_1), \ldots, f_n(\tilde{s}_n)$ and $g_1(\tilde{r}_1), \ldots, g_m(\tilde{r}_m)$.



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- Let it be h_1, \ldots, h_k .
- Then a rigid generalization of the given hedges has a form

 $X_1, h_1(\tilde{q}_1), X_2, h_2(\tilde{q}_2), \ldots, X_{k-1}, h_k(\tilde{q}_k), X_k,$



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where

- X's are (not necessarily distinct) new hedge variables,
- Some X's can be omitted,
- if $h_i = f_j = g_l$, then \tilde{q}_i is a rigid generalization of \tilde{s}_j and \tilde{r}_l .

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- The algorithm is parametrized by a rigidity function. It decides which common subsequences are taken.



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Rigidity function computes longest common subsequences.



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• Anti-unification equations:

$$X: \tilde{s} \triangleq \tilde{r},$$

meaning: X is a generalization of \tilde{s} and \tilde{r} .

The rule-based algorithm works on triples:

 $A; S; \sigma,$

where A is a set of anti-unification equations, S is a set of already solved anti-unification equations, σ is a substitution computed so far.

 \mathcal{R} : The rigidity function.

 \mathcal{R} -Dec-H: \mathcal{R} -Rigid Decomposition for Hedges

$$\begin{split} \{X:\tilde{s} \triangleq \tilde{q}\} \cup A; \ S; \ \sigma \Longrightarrow \\ \{Z_k:\tilde{s}_k \triangleq \tilde{q}_k \mid 1 \le k \le n\} \cup A; \\ \{Y_0:\tilde{s}|_0^{i_1} \triangleq \tilde{q}|_0^{j_1}\} \cup \{Y_k:\tilde{s}|_{i_k}^{i_{k+1}} \triangleq \tilde{q}|_{j_k}^{j_{k+1}} \mid 1 \le k \le n-1\} \cup \\ \{Y_n:\tilde{s}|_{i_n}^{|\tilde{s}|+1} \triangleq \tilde{q}|_{j_n}^{|\tilde{q}|+1}\} \cup S; \\ \sigma\{X \mapsto Y_0, f_1(Z_1), Y_1, \dots, Y_{n-1}, f_n(Z_n), Y_n\}, \end{split}$$

if $\mathcal{R}(top(\tilde{s}), top(\tilde{q}))$ contains a sequence $f_1[i_1, j_1] \cdots f_n[i_n, j_n]$ such that for all $1 \leq k \leq n$, $\tilde{s}|_{i_k} = f_k(\tilde{s}_k)$, $\tilde{q}|_{j_k} = f_k(\tilde{q}_k)$, and Y_0 , Y_k 's and Z_k 's are fresh.

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$$\mathcal{R}\text{-S-H: } \mathcal{R}\text{-Rigid Solve for Hedges}$$
$$\{X: \tilde{s} \triangleq \tilde{q}\} \cup A; \ S; \ \sigma \Longrightarrow A; \ \{X: \tilde{s} \triangleq \tilde{q}\} \cup S; \ \sigma,$$
if $\mathcal{R}(top(\tilde{s}), top(\tilde{q})) = \emptyset.$

 $\mathcal{R}\text{-}\mathsf{CS1:}\ \mathcal{R}\text{-}\textbf{Rigid}\ \textbf{Clean}\ \textbf{Store}\ \textbf{1}$

$$\begin{array}{l} \mathsf{A}; \; \{X_1: \tilde{s} \triangleq \tilde{q}, X_2: \tilde{s} \triangleq \tilde{q}\} \cup \mathsf{S}; \; \sigma \Longrightarrow \\ \mathsf{A}; \; \{X_1: \tilde{s} \triangleq \tilde{q}\} \cup \mathsf{S}; \; \sigma\{X_2 \mapsto X_1\}. \end{array}$$

 $\mathcal{R}\text{-}\mathsf{CS2:}\ \mathcal{R}\text{-}\mathsf{Rigid}\ \mathsf{Clean}\ \mathsf{Store}\ 2$

$$A; \ \{X : \epsilon \triangleq \epsilon\} \cup S; \ \sigma \Longrightarrow A; \ S; \ \sigma\{X \mapsto \epsilon\}.$$

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 $\mathcal{R}\text{-}\mathsf{CS3:}\ \mathcal{R}\text{-}\textbf{Rigid}\ \textbf{Clean}\ \textbf{Store}\ \textbf{3}$

$$A; \{x_1 : I \triangleq r, x_2 : I \triangleq r\} \cup S; \sigma \Longrightarrow$$
$$A; \{x_1 : I \triangleq r\} \cup S; \sigma\{x_2 \mapsto x_1\}.$$

\mathcal{R} -CS4: \mathcal{R} -Rigid Clean Store 4

$$\begin{array}{l} \mathsf{A}; \; \{X: I_1, \ldots, I_n \triangleq r_1, \ldots, r_n\} \cup \mathsf{S}; \; \sigma \Longrightarrow \\ \mathsf{A}; \; \{x_1: I_1 \triangleq r_1, \ldots, x_n: I_n \triangleq r_n\} \cup \mathsf{S}; \; \sigma\{X \mapsto x_1, \ldots, x_n\}, \end{array}$$

where $n \ge 1$ and x_i 's are fresh.

Rigid Unranked Anti-Unification Algorithm: Control

Given a rigidity function *R*, to compute *R*-generalizations of hedges s̃ and q̃, start with {*X* : s̃ ≜ q̃}; ∅; *Id* and apply the rules exhaustively.

Rigid Unranked Anti-Unification Algorithm: Properties

Theorem (Termination)

The algorithm terminates on any input and produces a system \emptyset ; *S*; σ .

Theorem (Soundness)

If the algorithm produces the derivation

$$\{X: \tilde{s}_1 \triangleq \tilde{s}_2\}; \emptyset; Id \Longrightarrow^* \emptyset; S; \sigma$$

then $X\sigma$ is a rigid generalization of \tilde{s}_1 and \tilde{s}_2 .

Theorem (Completeness)

Let \tilde{q} be a rigid generalization of \tilde{s}_1 and \tilde{s}_2 . Then the algorithm computes a rigid anti-unifier σ for $X : \tilde{s}_1 \triangleq \tilde{s}_2$ such that $\tilde{q} \preceq X\sigma$.

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Example

- \mathcal{R} computes the set of longest common subsequences.
- ▶ *R*-generalization of the hedges f(a, a), f(c), g(f(a), f(a)) and f(b, b), g(f(a), f).

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- Create the initial system:

 $\{X: f(a,a), f(c), g(f(a), f(a)) \triangleq f(b,b), g(f(a), f)\}, \emptyset, Id.$

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Obtain two terminal systems:

1.
$$\emptyset$$
, { $x : a \triangleq b, Y : f(c) \triangleq \epsilon, Z : a \triangleq \epsilon$ };
{ $X \mapsto f(x, x), Y, g(f(a), f(Z))$ }
2. \emptyset , { $Y : f(a, a) \triangleq \epsilon, Z : c \triangleq b, b, U : a \triangleq \epsilon$ };
{ $X \mapsto Y, f(Z), g(f(a), f(U))$ }

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The store tells how to obtain each original hedge from the generalization.

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Rigid Anti-Unification: Some Interesting Facts

- By choosing appropriate rigidity functions, rigid unranked anti-unification can model various existing generalization algorithms:
 - Simple hedge anti-unification for inductive reasoning over semi-structured documents (Yamamoto et al., 2001).
 - Word anti-unification (Cicekli and Ciceckli, 2006).
 - ϵ -free word anti-unification (Biere, 2003).
 - First-order anti-unification (Plotkin, 1972, Reynolds, 1972).
- Combination of rigid and complete (non-rigid) anti-unification algorithms can simulate AU anti-unification (Alpuente et al., 2008)

Unranked representation of code pieces:

$$\begin{array}{lll} \text{if}(>=(a, b), & \text{if}(>=(m, n), \\ \text{then}(=(c, +(d, b)), & \text{then}(=(y, +(x, n)), \\ =(d, +(d, 1))), & =(z, 1), \\ \text{else}(=(c, -(d, a)))) & =(x, +(x, 5))), \\ \text{else}(=(y, -(x, m))) \end{array}$$

An interesting generalization:

► { $y1 \mapsto a, y2 \mapsto b, y3 \mapsto c, y4 \mapsto d, y5 \mapsto 1, Y \mapsto \epsilon$ }

▶ $\{y1 \mapsto m, y2 \mapsto n, y3 \mapsto y, y4 \mapsto x, y5 \mapsto 5, Y \mapsto =(z, 1)\}$

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Rigid generalisation comes as a way to express many (maybe all) interesting practical techniques [of clone detection].

Anonymous referee of (Kutsia, Levy, Villaret, 2011)

- Rigid anti-unification helps to detect inserted or deleted pieces of code, which is necessary for clones of type 3.
- If we are interested in clones whose length is greater than a predefined threshold, we can include this measure in the definition of the rigidity function.
- The approach is modular, where most of the computations are performed on strings. It may combine advantages of fast textual and precise structural techniques and consider rigidity functions modulo a given metrics.

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- Anti-unifiers reflect similarities between two inputs, while the store reflects differences between them.
- The output of anti-unification can be used for comparison utilities and for extracting a procedure. This process has a use in code refactoring.
- Rigid anti-unification works on unranked terms that can abstract XML documents. How to detect clones well in XML/HTML is mentioned as one of the open problems in clone detection research in (Roy and Cordy, 2007).

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