

Problems Solved:

11	12	13	14	15
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Name:

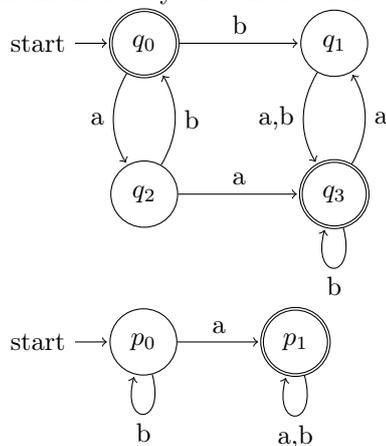
Matrikel-Nr.:

**Problem 11.** Let  $M_1 = (Q_1, \Sigma, \delta_1, q_1, F_1)$  and  $M_2 = (Q_2, \Sigma, \delta_2, q_2, F_2)$  be two DFSM over the alphabet  $\Sigma$ . Let  $L(M_1)$  and  $L(M_2)$  be the languages accepted by  $M_1$  and  $M_2$ , respectively.

Construct a DFSM  $M = (Q, \Sigma, \delta, q, F)$  whose language  $L(M)$  is the intersection of  $L(M_1)$  and  $L(M_2)$ . Write down  $Q$ ,  $\delta$ ,  $q$ , and  $F$  explicitly.

*Hint:*  $M$  simulates the parallel execution of  $M_1$  and  $M_2$ . For that to work,  $M$  “remembers” in its state the state  $M_1$  as well as the state of  $M_2$ . This can be achieved by defining  $Q = Q_1 \times Q_2$ .

Demonstrate your construction with the following DFSMs.

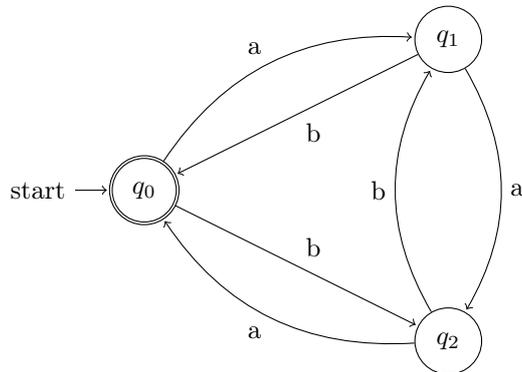


**Problem 12.** Answer the following questions:

- Is the language  $L := \{a^m b^n c^p \mid m, n, p \in \mathbb{N} \setminus \{0\}\}$  over the alphabet  $\Sigma = \{a, b, c\}$  regular?
- Is the language  $L = \{a^m b^n c^{m+n} \mid m, n \in \mathbb{N}\}$  over the alphabet  $\Sigma = \{a, b, c\}$  regular?

Justify your answers by giving a regular expression for the language or by using the Pumping Lemma.

**Problem 13.** Let  $M_1$  be the DFSM with states  $\{q_0, q_1, q_2\}$  whose transition graph is given below. Determine a regular expression  $r$  such that  $L(r) = L(M_1)$ . Show the *derivation* of the the final result by the technique based on Arden’s Lemma (see lecture notes).



**Problem 14.** Let  $r$  be the following regular expression.

$$(ab + ba)^* + bb$$

Construct a nondeterministic finite state machine  $N$  such that  $L(N) = L(r)$ . Show the derivation of the result by following the technique presented in the proof of the theorem *Equivalence of Regular Expressions and Automata* (see lecture notes).

**Problem 15.** Construct a Turing machine  $M = (Q, \Gamma, \sqcup, \{0, 1\}, \delta, q_0, F)$  such that  $L(M) = \{0^n 1^n \mid n \in \mathbb{N}^+\}$ . Write down  $Q$ ,  $\Gamma$ ,  $F$  and  $\delta$  explicitly.