

# **Praktische Softwaretechnologie**

**Lecture 6.**

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# **Math.round() and Math.random()**

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## **Static methods of class java.lang.Math**

public static long round(double a) – chooses the closer integer

public static int round(float a) – chooses the closer integer

public static double random() – generates a random floating point number between 0 and 1

# Math.round() and Math.random()

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## Usage:

- `Math.round(Math.random()*100)` – generates a long integer number between 0 and 100.
- `Math.round(Math.random()*99+1)` – generates a long integer number between 1 and 100.
- `Math.round(Math.random()*100/2)*2` – generates a **EVEN** long integer number between 0 and 100.
- `Math.round(Math.random()*98/2+1)*2` – generates a **EVEN** long integer number between 2 and 100.
- `Math.round(Math.random()*98/2+1)*2-1` – generates an **ODD** long integer number between 0 and 100 (1-99).

# Labyrinth

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Problem 1: Generate a labyrinth, from where there is one and only one way to get out (independently from the starting point).

Problem 2: Implement an algorithm which leads us out from the labyrinth (apply backtracking).

# Labyrinth

---

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```
import java.io.*;  
  
public class Labyrinth {  
  
    private final static ...      //Definitions of some constants  
  
    private static void horizontal(char[][] a, int x1, int y1, int x2, int y2) { ... }  
  
    private static void vertical(char[][] a, int x1, int y1, int x2, int y2) { ... }  
  
    private static void initMatrix(char[][] a) { ... }  
  
    private static void printOut(char[][] a) { ... }  
  
    private static boolean getOut(char[][] a, int x, int y) { ... }  
  
    public static void main(String[] args) { ... }  
}
```

# Labyrinth - Constants

---

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```
import java.io.*;  
  
public class Labyrinth {  
    private final static char WALL ='#';  
    private final static char CORRIDOR = ' ';  
    private final static char ESCAPE = '.';  
    private final static int WIDTH = 75;  
    private final static int HEIGHT = 25;  
    private final static int EXITX = HEIGHT-2;  
    private final static int EXITY = WIDTH-1;
```

...

# Labyrinth – method *main*

---

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```
public static void main(String[] args) {  
    char[][] a = new char[HEIGHT][WIDTH];  
    initMatrix(a);  
    horizontal(a, 0, 0, HEIGHT-1, WIDTH-1);  
  
    int x = (int)(Math.round(Math.random()*((HEIGHT-1-2)/2))+1)*2-1;  
    int y = (int)(Math.round(Math.random()*((WIDTH-1-2)/2))+1)*2-1;  
    a[x][y]=ESCAPE;  
    printOut(a);  
    System.out.println("Press Enter to continue!");  
    try {  
        System.in.read();  
    } catch (IOException e) {}  
    getOut(a,x,y);  
    printOut(a);  
}
```

# Labirinth – method *initMatrix*

---

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```
private static void initMatrix(char[][] a) {  
    for (int i=0; i<WIDTH; i++)  
        a[0][i] = WALL;  
  
    for (int j=1; j<HEIGHT-1; j++) {  
        a[j][0]=WALL;  
        for (int i=1; i<WIDTH-1; i++) {  
            a[j][i]=CORRIDOR;  
        }  
        a[j][WIDTH-1]=WALL;  
    }  
  
    for (int i=0; i<WIDTH; i++)  
        a[HEIGHT-1][i] = WALL;  
  
    a[EXITX][EXITY]=CORRIDOR;  
}
```

It draws the walls of a room with one exit in the matrix.

# Labyrinth – method *printOut*

---

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```
private static void printOut(char[][] a) {  
    for (int j=0; j<HEIGHT; j++) {  
        for (int i=0; i<WIDTH; i++) {  
            System.out.print(a[j][i]);  
        }  
        System.out.println();  
    }  
}
```

# Labyrinth – method *horizontal*

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```
private static void horizontal (char[][] a, int x1, int y1, int x2, int y2) {  
    int j = (int)(Math.round(Math.random()*((y2-y1-4)/2))+1)*2;  
    for(int i=x1; i<=x2; i++) {  
        a[i][y1+j]=WALL;  
    }  
    int i = (int)(Math.round(Math.random()*((x2-x1-2)/2))+1)*2-1;  
    a[x1+i][y1+j]=CORRIDOR;  
  
    if (j > 2) vertical(a, x1, y1, x2, y1+j);  
    if (y2-y1-j > 2) vertical(a, x1, y1+j, x2, y2);  
}
```

**It divides a (sub)room to two parts with a vertical line/wall and open a gateway on it.**

# Labyrinth – method *vertical*

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```
private static void vertical(char[][] a, int x1, int y1, int x2, int y2) {  
    int j = (int)(Math.round(Math.random()*((x2-x1-4)/2))+1)*2;  
    for(int i=y1; i<=y2; i++) {  
        a[x1+j][i]=WALL;  
    }  
    int i = (int)(Math.round(Math.random()*((y2-y1-2)/2))+1)*2-1;  
    a[x1+j][y1+i]=CORRIDOR;  
  
    if (j > 2) horizontal(a, x1, y1, x1+j, y2);  
    if (x2-x1-j > 2) horizontal(a, x1+j, y1, x2, y2);  
}
```

**It divides a (sub)room to two parts with a horizontal line/wall and open a gateway on it.**

# Labyrinth – method *getOut*

---

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```
private static boolean getOut(char[][] a, int x, int y) {  
    if (x==0 || y==0 || x==HEIGHT-1 || y==WIDTH-1) {  
        return true;  
    }  
  
    boolean success = false;  
    a[x][y] = ESCAPE;  
  
    if (a[x-1][y] == CORRIDOR) success = getOut(a, x-1, y);  
    if (!success && a[x][y-1] == CORRIDOR) success = getOut(a, x, y-1);  
    if (!success && a[x+1][y] == CORRIDOR) success = getOut(a, x+1, y);  
    if (!success && a[x][y+1] == CORRIDOR) success = getOut(a, x, y+1);  
  
    if (!success) a[x][y]=CORRIDOR; // tidy up  
  
    return success;  
}
```

Typical application of backtracking!

# Labyrinth – Output 1.

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# Labyrinth – Output 2.

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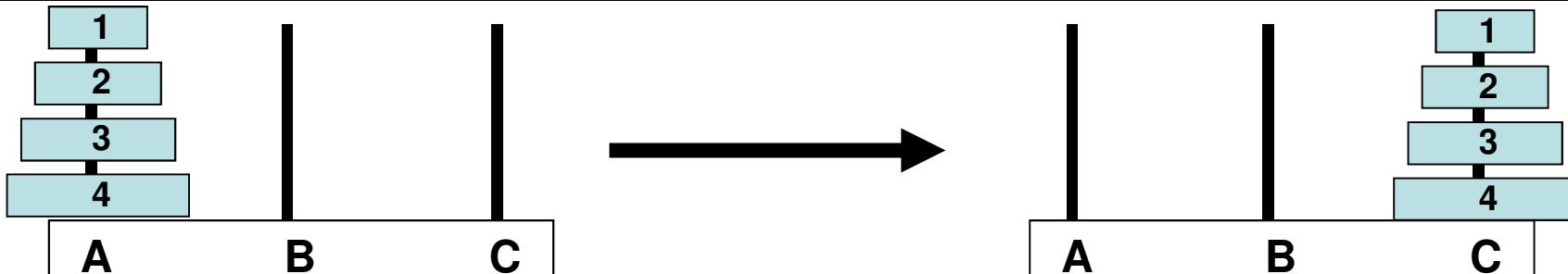
Press Enter to continue!

D:\tmp>

# Exercise 7 – Towers of Hanoi

Deadline: 30.04.2014

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You must place all rings from the stick A to the stick C in the same order with the help of stick B, such that:

- You can move only one ring in one step from a stick to another
- You can put a ring only either on an empty stick or on a top of another ring whose diameter is bigger.
- The program prints out the movement of a ring in each step, e.g.: “Move the 3. ring from A to B!”

You must implement a recursive algorithms for the problem.

# Definite Integral

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**Problem:** Compute (more or less precisely) the definite integral of function  $\sin(x)/x$  between 0.1 and 10.

**How:** The value of the definite integral of a function within a predefined interval is equal to the area under of the function curve → We will approach this area with areas of trapezes.

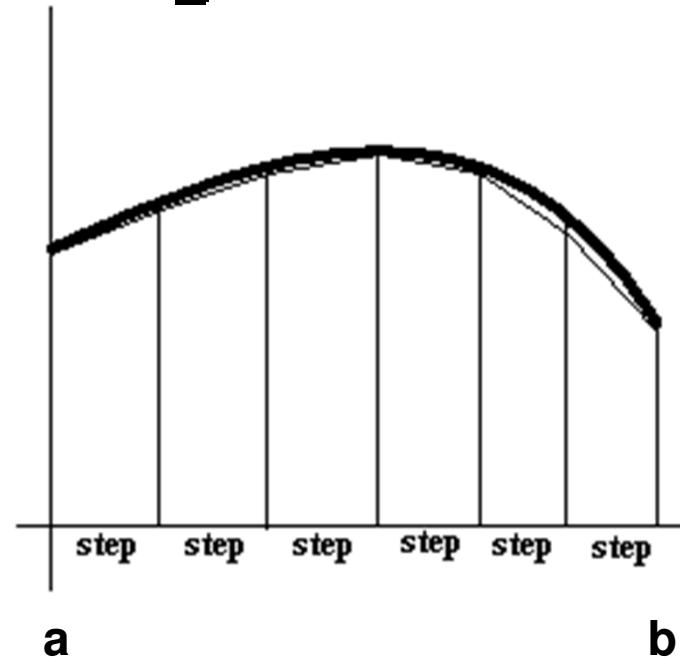


# Definite Integral

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$$T_n = \frac{f(a) + f(a+s)}{2}s + \frac{f(a+s) + f(a+2s)}{2}s + \dots + \frac{f(a+(n-1)s) + f(b)}{2}s$$

$$T_n = s \left[ \frac{f(a)}{2} + \frac{f(a+s) + f(a+2s) + \dots + f(a+(n-1)s) + f(b)}{2} \right]$$



# Definite Integral

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```
public class DefiniteIntegral1 {  
    public static void main(String args[]) {  
        double bottomX = 0.1;  
        double topX= 10;  
        double area = (Math.sin(bottomX)/bottomX + Math.sin(topX)/topX) / 2;  
  
        if (args.length == 0) return;  
        int n = Integer.parseInt(args[0]);  
  
        double step = (topX-bottomX)/n;  
        double x = bottomX + step;  
  
        for (int k = 1; k < n; k++) {  
            area += Math.sin(x)/x;  
            x += step;  
        }  
        area *= step;  
        System.out.println("The definite integral of sin(x)/x between " + bottomX + "  
and " + topX + " is " + area);  
    }  
}
```

# Definite Integral - Output

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```
D:\>cd tmp

D:\tmp>java DefiniteIntegral1 10
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.4107173602374352

D:\tmp>java DefiniteIntegral1 100
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5468605464223368

D:\tmp>java DefiniteIntegral1 1000
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5573179459717392

D:\tmp>java DefiniteIntegral1 10000
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5582953363702468

D:\tmp>java DefiniteIntegral1 100000
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5583923606852785

D:\tmp>java DefiniteIntegral1 1000000
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5584020559400473

D:\tmp>java DefiniteIntegral1 10000000
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.558403025326189

D:\tmp>
```

# Definite Integral 2 with Given Precision

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---

**Problem:** Compute the definite integral of function  $\sin(x)/x$  between 0.1 and 10 with a given decimal precision.

# Definite Integral 2

---

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```
public class DefiniteIntegral2 {  
    public static void main(String args[]) {  
        double bottomX = 0.1;  
        double topX= 10;  
        double area = 0;  
        double prevArea;  
        int n = 10;  
  
        if (args.length == 0) return;  
        double precision = Double.parseDouble(args[0]);  
        ...  
    }  
}
```

# Definite Integral 2

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```
do {  
    prevArea = area;  
  
    area = (Math.sin(bottomX)/bottomX + Math.sin(topX)/topX) / 2;  
    double step = (topX-bottomX)/n;  
    double x = bottomX + step;  
  
    for (int k = 1; k < n; k++) {  
        area += Math.sin(x)/x;  
        x += step;  
    }  
    area *= step;  
    n *= 10;  
} while (Math.abs(area-prevArea) > precision);  
  
System.out.println("The definite integral of sin(x)/x between " + bottomX + "  
and " + topX + " is " + area);  
}
```

# Definite Integral 2 - Output

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```
D:\>cd tmp  
D:\tmp>java DefiniteIntegral2 0.1  
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5573179459717392  
D:\tmp>java DefiniteIntegral2 0.01  
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5582953363702468  
D:\tmp>java DefiniteIntegral2 0.001  
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5582953363702468  
D:\tmp>java DefiniteIntegral2 0.0001  
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5583923606852785  
D:\tmp>java DefiniteIntegral2 0.00001  
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.5584020559400473  
D:\tmp>java DefiniteIntegral2 0.000001  
The definite integral of sin(x)/x between 0.1 and 10.0 is 1.558403025326189  
D:\tmp>  
D:\tmp>  
D:\tmp>  
D:\tmp>
```

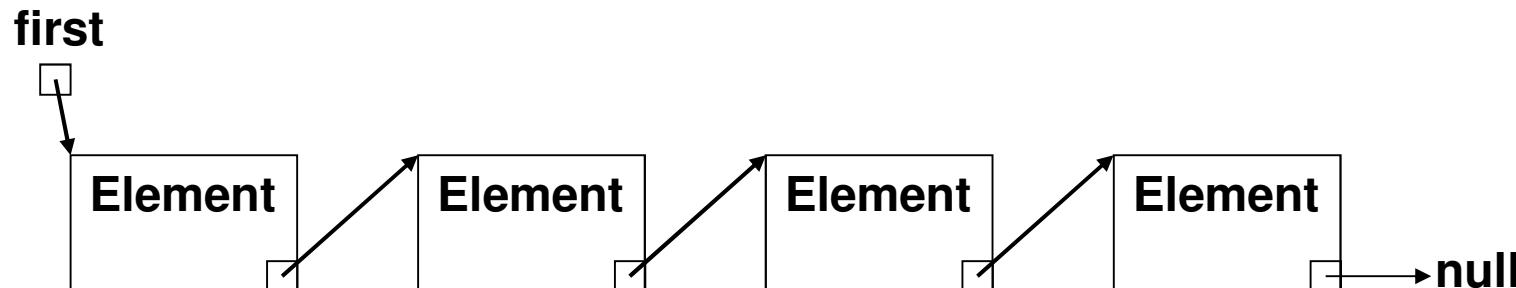
# Stack Made from a Linked List

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Problem: Create a stack where the maximum number of its element is not predefined.

How: Apply a list of objects, where an object always refers to the subsequent object via one of its data field.

Another advantages: Memory is allocated only for the existing elements.



# Stack Made from a Linked List

---

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```
public class StackElement {  
    private String value;  
    private StackElement next;  
  
    public StackElement(String value, StackElement next) {  
        this.value = value;  
        this.next = next;  
    }  
  
    public String getValue() {  
        return value;  
    }  
  
    public StackElement getNext() {  
        return next;  
    }  
}
```

# Stack Made from a Linked List

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```
public class LinkedListStack {  
  
    private StackElement top;  
  
    public LinkedListStack() {  
        top = null;  
    }  
  
    public void push(String s) {  
        StackElement tmp = new StackElement(s, top);  
        top = tmp;  
    }  
  
    public String pop() {  
        StackElement tmp = top;  
        top = tmp.getNext();  
        return tmp.getValue();  
    }  
}
```

```
public boolean isEmpty() {  
    if (top==null) return true;  
    return false;  
}  
  
public String toString() {  
    StringBuilder sb =new StringBuilder();  
    StackElement tmp = top;  
    while (tmp !=null) {  
        sb.append(tmp.getValue()+" ");  
        tmp = tmp.getNext();  
    }  
    return sb.toString();  
}  
}
```

# Stack Made from a Linked List

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```
public class Test {  
    public static void main(String[] args) {  
        LinkedListStack stack1 = new LinkedListStack(); //no given size  
        LinkedListStack stack2 = new LinkedListStack(); //no given size  
  
        stack1.push("Tom");  
        stack1.push("Tim");  
        stack1.push("Tracy");  
        stack1.push("George");  
  
        System.out.println("The content of the 1. stack:" + stack1);  
  
        while (!stack1.isEmpty()) {  
            stack2.push(stack1.pop());  
        }  
  
        System.out.println("The content of the 2. stack:" + stack2);  
    }  
}
```

# Stack Made from a Linked List - Output

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```
Microsoft Windows XP [Version 5.1.2600]
(C) Copyright 1985-2001 Microsoft Corp.

C:\Documents and Settings\Karoly Bosa>d:

D:>>cd tmp

D:\tmp>cd LinkedListStack

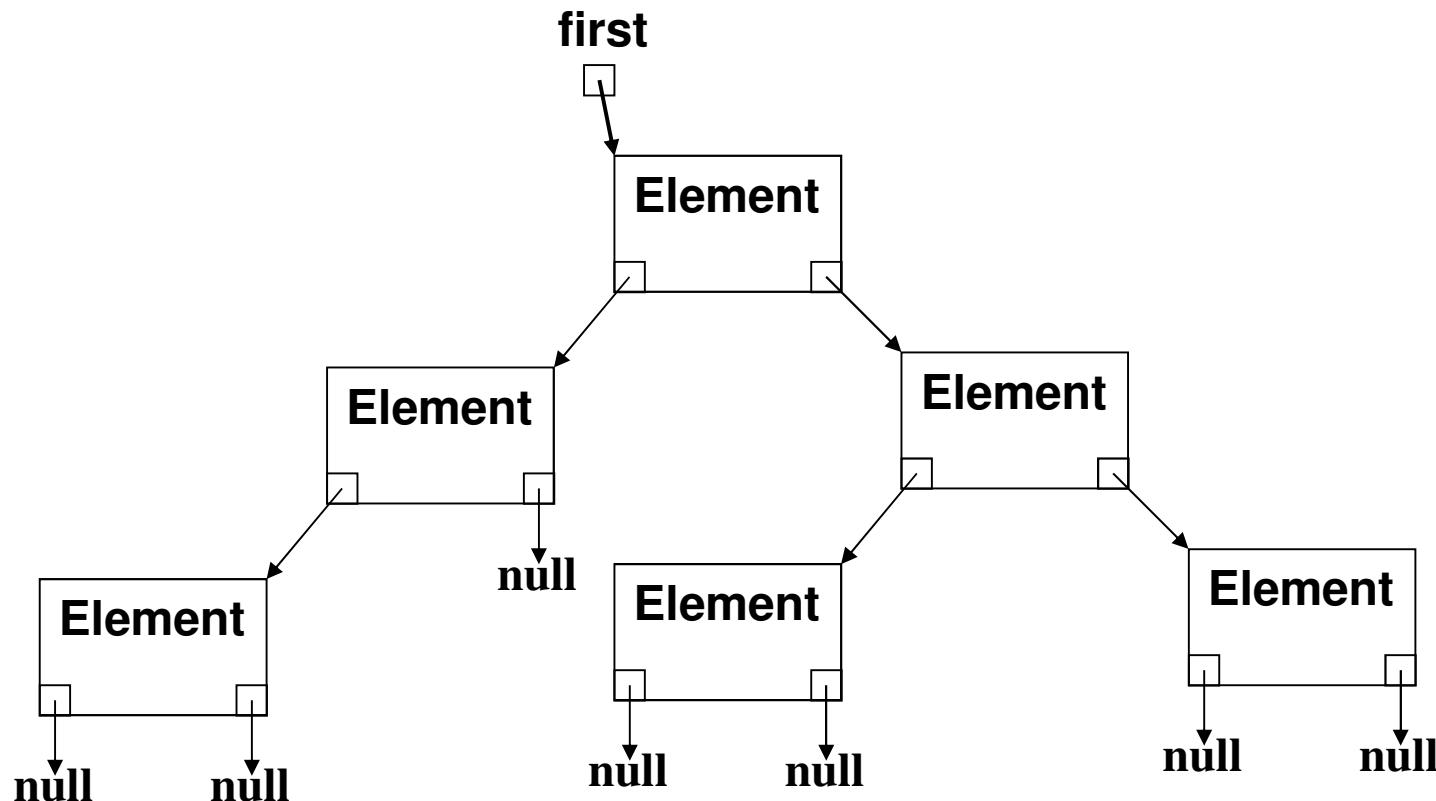
D:\tmp\LinkedListStack>
D:\tmp\LinkedListStack>java Test
The content of the 1. stack:George Tracy Tim Tom
The content of the 2. stack:Tom Tim Tracy George

D:\tmp\LinkedListStack>_
```

# Binary Trees

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A linked data structure is called binary tree, if each element is followed at most two subsequent elements.

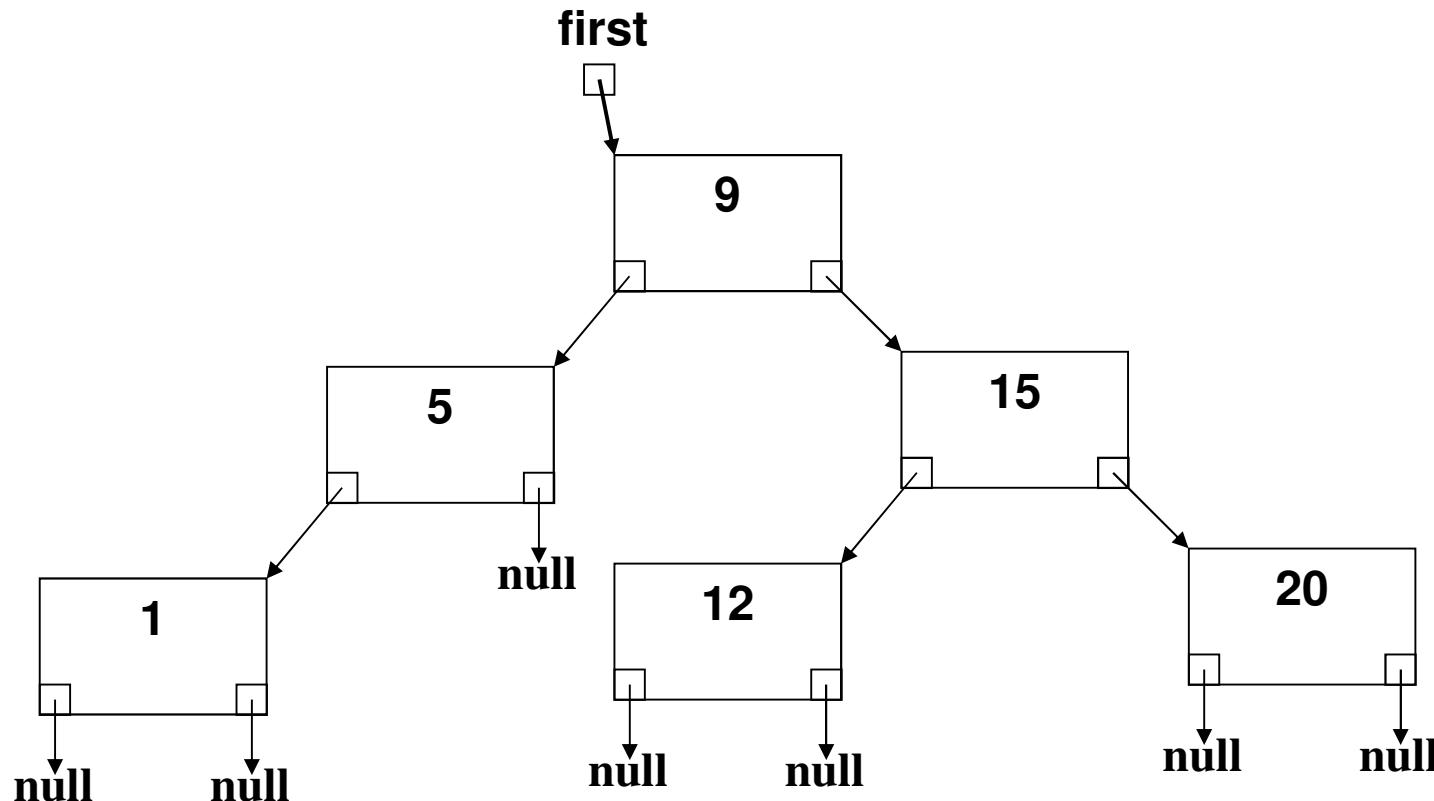


# Binary Search Trees

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A binary tree is a search tree, if each node fulfills that:

- its value is greater than all values stored in its left sub-tree.
- its value is less than all values stored in its right sub-tree.



# Binary Search Trees – class TreeElement

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```
public class TreeElement {  
    private int value;  
    private TreeElement left, right;  
  
    public TreeElement(int value) {  
        this.value = value;  
        this.left = null;  
        this.right = null;  
    }  
  
    public int getValue() {  
        return value;  
    }  
  
    public TreeElement getLeft() {  
        return left;  
    }  
  
    public TreeElement getRight() {  
        return right;  
    }  
}
```

```
public void setLeft(TreeElement left) {  
    this.left=left;  
}  
  
public void setRight(TreeElement right) {  
    this.right=right;  
}  
  
public String toString() {  
    StringBuilder sb = new  
        StringBuilder();  
    if (left != null)  
        sb.append(left.toString());  
    sb.append(value+" ");  
    if (right != null)  
        sb.append(right.toString());  
    return sb.toString();  
}  
}
```

# Binary Search Trees – class BinarySearchTree

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```
public class BinarySearchTree {  
  
    private TreeElement root;  
  
    public BinarySearchTree() {  
        root = null;  
    }  
  
    public boolean isEmpty() {  
        if (root==null) return true;  
        return false;  
    }  
  
    public String toString() {  
        if (root != null) {  
            return root.toString();  
        }  
        return "";  
    }  
}
```

# Binary Search Trees – class BinarySearchTree

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```
public void insert(int value) {
    boolean inserted = false;
    TreeElement newElement = new TreeElement(value);
    if (root==null) { root = newElement;}
    else {
        TreeElement tmp = root;
        while (!inserted) {

            if (tmp.getValue() == value) {inserted = true;}
            else if (tmp.getValue() > value) {
                if (tmp.getLeft() != null) {tmp = tmp.getLeft();}
                else { tmp.setLeft(newElement); inserted = true;}
            }
            else {
                if (tmp.getRight() != null) {tmp = tmp.getRight();}
                else { tmp.setRight(newElement); inserted = true;}
            }
        }
    }
}
```

# Binary Search Trees – class Test

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```
public class Test {  
    public static void main(String[] args) {  
        BinarySearchTree tree = new BinarySearchTree();  
  
        tree.insert(47);  
        tree.insert(74);  
        tree.insert(21);  
        tree.insert(99);  
        tree.insert(51);  
        tree.insert(15);  
        tree.insert(65);  
        tree.insert(36);  
        tree.insert(83);  
        tree.insert(59);  
  
        System.out.println("The content of the tree by an \"inorder\" ranging is " + tree);  
    }  
}
```

# Exercise 8 – Extend the Search Tree

---

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Extend the class *BinarySearchTree* with a method  
*String search(int n)*, which search n in the tree. The method  
returns the description, how to get to n.

E.g.:

Input: n = 11

Output: “Root:16 Left 5 Right 10 Right 11”

Test the *search() method!*

Deadline: 30.04.2014