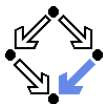
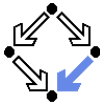


# Verifying Java Programs with KeY

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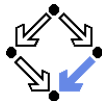
# Verifying Java Programs

---

- **Extended static checking of Java programs:**
  - Even if no error is reported, a program may violate its specification.
    - Unsound calculus for verifying while loops.
  - Even correct programs may trigger error reports:
    - Incomplete calculus for verifying while loops.
    - Incomplete calculus in automatic decision procedure (Simplify).
- **Verification of Java programs:**
  - Sound verification calculus.
    - Not unfolding of loops, but loop reasoning based on invariants.
    - Loop invariants must be typically provided by user.
  - Automatic generation of verification conditions.
    - From JML-annotated Java program, proof obligations are derived.
  - Human-guided proofs of these conditions (using a proof assistant).
    - Simple conditions automatically proved by automatic procedure.

We will now deal with an integrated environment for this purpose.

# The KeY Tool

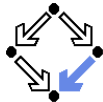


<http://www.key-project.org>

- **KeY:** environment for verification of JavaCard programs.
  - Subset of Java for smartcard applications and embedded systems.
  - Universities of Karlsruhe, Koblenz, Chalmers, 1998–
    - Beckert et al: “Verification of Object-Oriented Software: The KeY Approach”, Springer, 2007. (book)
    - Ahrendt et al: “The KeY Tool”, 2005. (paper)
    - Engel and Roth: “KeY Quicktour for JML”, 2006. (short paper)
- **Specification languages:** OCL and JML.
  - Original: OCL (Object Constraint Language), part of UML standard.
  - Later added: JML (Java Modeling Language).
- **Logical framework:** Dynamic Logic (DL).
  - Successor/generalization of Hoare Logic.
  - Integrated prover with interfaces to external decision procedures.
    - Simplify, ICS, CVC3, CVCLite, Yices, ...

We will only deal with the tool's JML interface “JMLKeY”.

# Dynamic Logic



Further development of Hoare Logic to a modal logic.

- **Hoare logic:** two separate kinds of statements.
  - Formulas  $P, Q$  constraining program states.
  - Hoare triples  $\{P\}C\{Q\}$  constraining state transitions.
- **Dynamic logic:** single kind of statement.

Predicate logic formulas extended by two kinds of modalities.

- $[C]Q$  ( $\Leftrightarrow \neg\langle C\rangle\neg Q$ )
  - Every state that can be reached by the execution of  $C$  satisfies  $Q$ .
  - The statement is trivially true, if  $C$  does not terminate.
- $\langle C\rangle Q$  ( $\Leftrightarrow \neg[C]\neg Q$ )
  - There exists some state that can be reached by the execution of  $C$  and that satisfies  $Q$ .
  - The statement is only true, if  $C$  terminates.

States and state transitions can be described by DL formulas.

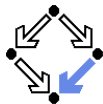
# Dynamic Logic versus Hoare Logic



Hoare triple  $\{P\}C\{Q\}$  can be expressed as a DL formula.

- **Partial correctness interpretation:**  $P \Rightarrow [C]Q$ 
  - If  $P$  holds in the current state and the execution of  $C$  reaches another state, then  $Q$  holds in that state.
  - Equivalent to the partial correctness interpretation of  $\{P\}C\{Q\}$ .
- **Total correctness interpretation:**  $P \Rightarrow \langle C \rangle Q$ 
  - If  $P$  holds in the current state, then there exists another state that can be reached by the execution of  $C$  in which  $Q$  holds.
  - If  $C$  is deterministic, there exists at most one such state; then equivalent to the total correctness interpretation of  $\{P\}C\{Q\}$ .

For deterministic programs, the interpretations coincide.



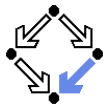
# Advantages of Dynamic Logic

---

Modal formulas can also occur in the context of quantifiers.

- **Hoare Logic:**  $\{x = a\} y := x * x \{x = a \wedge y = a^2\}$ 
  - Use of free mathematical variable  $a$  to denote the “old” value of  $x$ .
- **Dynamic logic:**  $\forall a : x = a \Rightarrow [y := x * x] x = a \wedge y = a^2$ 
  - Quantifiers can be used to restrict the scopes of mathematical variables across state transitions.

Set of DL formulas is closed under the usual logical operations.



# A Calculus for Dynamic Logic

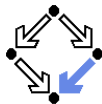
## ■ A core language of commands (non-deterministic):

$X := T$  ... assignment  
 $C_1; C_2$  ... sequential composition  
 $C_1 \cup C_2$  ... non-deterministic choice  
 $C^*$  ... iteration (zero or more times)  
 $F?$  ... test (blocks if  $F$  is false)

## ■ A high-level language of commands (deterministic):

**skip** = true?  
**abort** = false?  
 $X := T$   
 $C_1; C_2$   
**if**  $F$  **then**  $C_1$  **else**  $C_2$  =  $(F?; C_1) \cup ((\neg F)?; C_2)$   
**if**  $F$  **then**  $C$  =  $(F?; C) \cup (\neg F)?$   
**while**  $F$  **do**  $C$  =  $(F?; C)^*; (\neg F)?$

A calculus is defined for dynamic logic with the core command language.



# A Calculus for Dynamic Logic

## Basic rules:

- Rules for predicate logic extended by general rules for modalities.

## Command-related rules:

- $$\frac{\Gamma \vdash F[T/X]}{\Gamma \vdash [X := T]F}$$
- $$\frac{\Gamma \vdash [C_1][C_2]F}{\Gamma \vdash [C_1; C_2]F}$$
- $$\frac{\Gamma \vdash [C_1]F \quad \Gamma \vdash [C_2]F}{\Gamma \vdash [C_1 \cup C_2]F}$$
- $$\frac{\Gamma \vdash F \quad \Gamma \vdash [C^*](F \Rightarrow [C]F)}{\Gamma \vdash [C^*]F}$$
- $$\frac{\Gamma \vdash F \Rightarrow G}{\Gamma \vdash [F?]G}$$

From these, Hoare-like rules for the high-level language can be derived.



# Objects and Updates



Calculus has to deal with the pointer semantics of Java objects.

- **Aliasing:** two variables  $o, o'$  may refer to the same object.
  - Field assignment  $o.a := T$  may also affect the value of  $o'.a$ .
- **Update formulas:**  $\{o.a \leftarrow T\}F$ 
  - Truth value of  $F$  in state after the assignment  $o.a := T$ .

- **Field assignment rule:**

$$\frac{\Gamma \vdash \{o.a \leftarrow T\}F}{\Gamma \vdash [o.a := T]F}$$

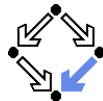
- **Field access rule:**

$$\frac{\Gamma, o = o' \vdash F(T) \quad \Gamma, o \neq o' \vdash F(o'.a)}{\Gamma \vdash \{o.a \leftarrow T\}F(o'.a)}$$

- Case distinction depending on whether  $o$  and  $o'$  refer to same object.
- Only applied as last resort (after all other rules of the calculus).

Considerable complication of verifications.

# The JMLKeY Prover



/zvol/formal/bin/startProver &

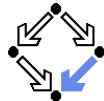
The screenshot displays the JMLKeY Prover interface. The main window is titled "KeY -- Prover" and contains several panes:

- Tasks:** Shows the current model and goals, such as "with model paycard@17:12:06 #1" and "Ensures Post Condition PO (using only invariants from Pa)".
- Proof Search Strategy:** A table with columns for "Proof", "Goals", and "User Constraint".
- Rules:** A table with columns for "Proof", "Goals", and "User Constraint".
- Proof Tree:** A hierarchical tree of proof steps. The current goal is highlighted in blue, and the steps leading to it are highlighted in yellow. The current goal is:

```
self_LogFile_lv_0.logArray[i_0].balance >= 1 + max_0.balance,  
self_LogFile_lv_0.logArray[i_0].<created> = TRUE,  
i_0 <= 2,  
{i:=i_0 || max:=max_0}anon(i, max),  
i_0 >= 0,  
\forallall jint j;  
( j <= -1  
 | j >= i_0  
 | self_LogFile_lv_0.logArray[j].balance <= max_0.balance),  
self_LogFile_lv_0.<created> = TRUE,  
self_LogFile_lv_0.logArray.<created> = TRUE,  
self_LogFile_lv_0.logArray.length = 3,  
self_LogFile_lv_0.currentRecord <= 2,  
self_LogFile_lv_0.currentRecord >= 0,  
\forallall int index_lv_0;  
( index_lv_0 <= -1  
 | index_lv_0 >= 3  
 | !self_LogFile_lv_0.logArray[index_lv_0] = null),  
inReachableState  
==>  
max_0 = null,  
self_LogFile_lv_0.logArray = null,  
self_LogFile_lv_0 = null,  
self_LogFile_lv_0.logArray[i_0] = null,  
{i:=i_0 || max:=max_0}anon(i, max)  
& ( (jint)(1 + i_0) >= 0  
 & ( self_LogFile_lv_0.logArray.length >= (jint)(1 + i_0)  
 & ( !self_LogFile_lv_0.logArray[i_0] = null  
 & \forallall jint j;  
 cut_direct  
 local_cut  
 Apply rules automatically here  
 to clipboard  
 Create abbreviation
```
- Current Goal:** A text area showing the current goal and the steps leading to it. The current goal is highlighted in blue, and the steps leading to it are highlighted in yellow.

The status bar at the bottom indicates "Integrated Deductive Software Design: Ready".

# A Simple Example



Engel et al: “KeY Quicktour for JML”, 2005.

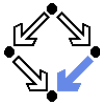
```
package paycard;

public class PayCard {

  /*@ public instance invariant
    @   log != null
    @   && balance >=0
    @   && limit >0
    @   && unsuccessfulOperations >=0;
  */

  /*@ spec_public @*/ int limit=1000;
  /*@ spec_public @*/
    int unsuccessfulOperations;
  /*@ spec_public @*/ int id;
  /*@ spec_public @*/ int balance=0;
  /*@ spec_public @*/
    protected LogFile log;

  /*@
    @ public normal_behavior
    @ requires amount>0 ;
    @ assignable
    @   unsuccessfulOperations, balance;
    @ ensures balance >= \old(balance);
  */
  public boolean charge(int amount) {
    if (this.balance+amount>=this.limit) {
      this.unsuccessfulOperations++;
      return false;
    } else {
      this.balance=this.balance+amount;
      return true;
    }
  }
  ...
}
```



## A Simple Example (Contd)

---

Choose in Menu "File/Load" a package directory or a KeY file.

```
// paycard.key
// This file is part of KeY - Integrated Deductive Software Design
// Copyright (C) 2001-2009 Universitaet Karlsruhe, Germany
//                               Universitaet Koblenz-Landau, Germany
//                               Chalmers University of Technology, Sweden
//
// The KeY system is protected by the GNU General Public License.
// See LICENSE.TXT for details.

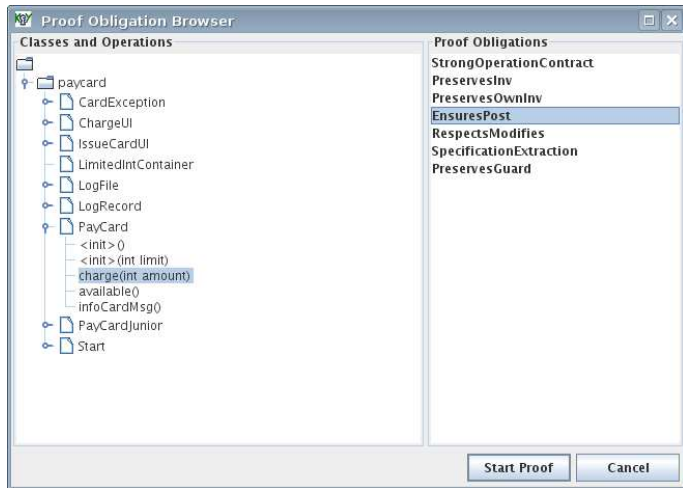
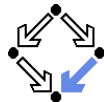
\classpath "classpath";

\javaSource "paycard";

\chooseContract;
```

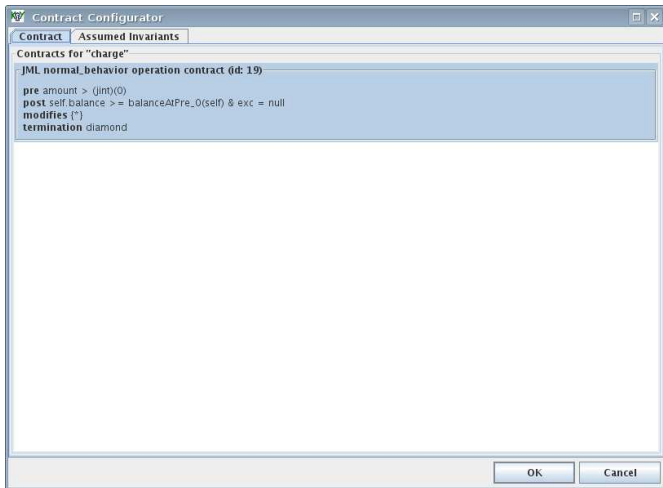
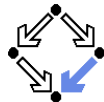
Needed (only) to look up sources of system classes.

## A Simple Example (Contd'2)



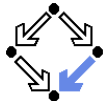
Generate the proof obligations and choose one for verification.

# A Simple Example (Contd'3)



Display the chosen proof obligation and start the proof.

# A Simple Example (Contd'4)

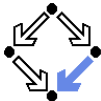


The screenshot shows the KeY Prover interface with the following components:

- Tasks:** Env. with model paycard@10:00:47 AM #1, EnsuresPost (paycard.PayCard.charge, JML normal).
- Proof Search Strategy:** Proof, Goals, User Constraint.
- Proof Tree:** 1: OPEN GOAL.
- Current Goal:** A complex Dynamic Logic formula involving quantifiers and conditions on `paycard` objects.

```
Current Goal
-> p_0.balance = p_0.log.getLogArray(p_0.log.getCurrentRecord().balance
)
& \forallall paycard.PayCard p_0;
( p_0.<created> = TRUE & lp_0 = null
-> p_0.log.currentRecord < p_0.log.getLogArray.Length
& ( p_0.log.currentRecord == (jint)0)
& ( lp_0.log.getLogArray == null
& \forallall jint i;
( 0 <= i & i <= p_0.log.getLogArray.Length
-> lp_0.log.getLogArray[i] = null)
& paycard.LogFile.logFileSize = p_0.log.getLogArray.Length
)))
& \forallall paycard.PayCard p_0;
(p_0.<created> = TRUE & lp_0 = null -> p_0.balance >= (jint)0))
& \forallall paycard.PayCard p_0;
(p_0.<created> = TRUE & lp_0 = null -> p_0.limit > (jint)0))
& \forallall paycard.PayCard p_0;
( p_0.<created> = TRUE & lp_0 = null
-> p_0.available@(paycard.PayCard)() >= (jint)0))
& \forallall paycard.PayCard p_0;
( p_0.<created> = TRUE & lp_0 = null
-> p_0.unsuccessfulOperations >= (jint)0))
& (self.<created> = TRUE & !self = null)
& inInt(amount)
& amount > (jint)0)
-> { _amount:=amount ||
\for paycard.PayCard x; balanceAtPre_0(x):=x.balance)
\<{
exc=null;try {
self.charge(_amount)@paycard.PayCard;
} catch (java.lang.Throwable e) {
exc=e;
}
}\> (self.balance >= balanceAtPre_0(self) & exc = null)
```

The proof obligation in Dynamic Logic.



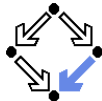
## A Simple Example (Contd'5)

```
==>
  inReachableState
-> \forall int amount_lv;
    {amount:=amount_lv}
    \forall paycard.PayCard self_PayCard_lv;
      {self_PayCard:=self_PayCard_lv}
      {_old13:=self_PayCard.balance}
      (
        !self_PayCard = null
        & self_PayCard.<created> = TRUE
        & amount > 0
        & ( !self_PayCard.log = null
            & ...
            & self_PayCard.balance >= 0
            & self_PayCard.limit > 0
            & self_PayCard.available@(paycard.PayCard)() >= 0
            & self_PayCard.unsuccessfulOperations >= 0)
      -> \{ {
          self_PayCard.charge(amount)@paycard.PayCard;
        }
      }\> self_PayCard.balance >= _old13
```

Press button "Start automated proof search".



# A Simple Example (Contd'6)



Key - Praver

File View Proof Options Tools About

Run Simplify Prune Proof Reuse

Tasks

Env. with model paycard@10:00:47 AM #1

EnsuresPost (paycard.PayCard.charge, JML normal)

Proof Search Strategy Rules

Proof	Goals	User Constraint
Proof		
1: eq_and_2		
2: insert_constant_value		
3: insert_constant_value		
4: inInt		
5: concrete_and_3		
6: impRight		
7: andLeft		
8: andLeft		
9: andLeft		
10: andLeft		
11: andLeft		
12: notLeft		
13: andLeft		
14: andLeft		
15: andLeft		
16: andLeft		
17: andLeft		
18: andLeft		
19: castDel		
20: castDel		
21: castDel		
22: castDel		
23: castDel		
24: castDel		

Inner Node

```
inReachableState
& \forall paycard.PayCard p_0;
  ( p_0.<created> = TRUE & !p_0 = null
  -> !p_0.log = null)
& \forall paycard.PayCard p_0;
  ( p_0.<created> = TRUE & !p_0 = null
  -> !p_0.log = null)
& \forall paycard.PayCard p_0;
  ( p_0.<created> = TRUE & !p_0 = null
  -> !p_0.log.currentRecord.balance
  < p_0.log.logArray.length
  & ( p_0.log.currentRecord >= (jint)0)
  & ( !p_0.log.logArray = null
  & \forall jint i;
    ( 0 <= i
    & i
    <= p_0.log.logArray.length
    -> !p_0.log.logArray[i] = null)
    & paycard.LogFile.logFileSize
    = p_0.log.logArray.length)))
& \forall paycard.PayCard p_0;
  ( p_0.<created> = TRUE & !p_0 = null
  -> p_0.balance >= (jint)0)
& \forall paycard.PayCard p_0;
  ( p_0.<created> = TRUE & !p_0 = null
  -> p_0.time >= (jint)0)
```

Proof closed

Proved.

Statistics:

Nodes: 731

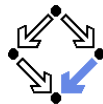
Branches: 12

OK

Strategy: Applied 719 rules (3.6 sec, closed 12 goals, 0 remaining)

Proof runs through automatically.

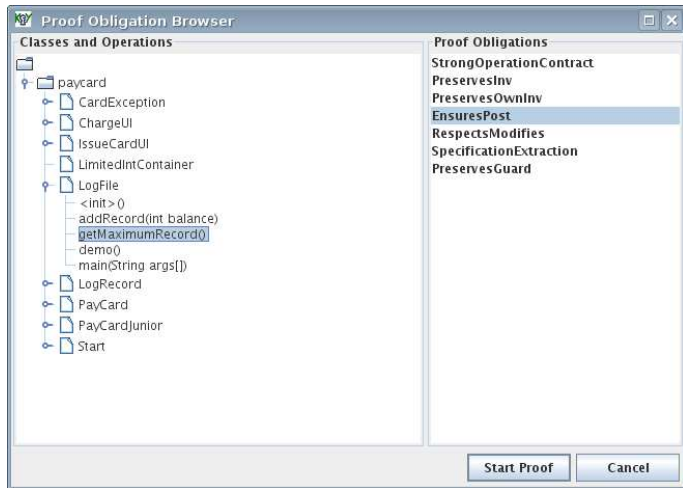
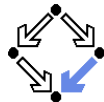
# A Loop Example



```
public class LogFile {
    /*@ public invariant
    @ logArray.length
    @ == logFileSize &&
    @ currentRecord < logFileSize
    @ && currentRecord >= 0 &&
    @ \nonnullElements(logArray);
    @*/
    private /*@ spec_public @*/
        static int logFileSize = 3;
    private /*@ spec_public @*/
        int currentRecord;
    private /*@ spec_public @*/
        LogRecord[] logArray =
            new LogRecord[logFileSize];
    ...
}

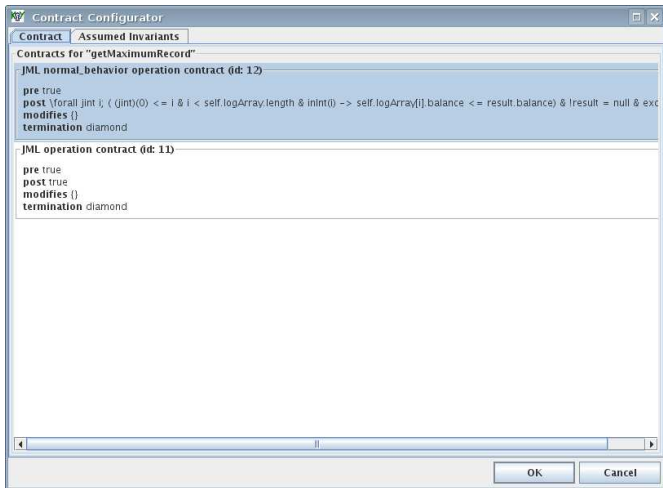
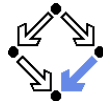
/*@ public normal_behavior
    @ ensures
    @ (\forall int i; 0 <= i && i < logArray.length;
    @   logArray[i].balance <= \result.balance); */
public /*@pure@*/
LogRecord getMaximumRecord(){
    LogRecord max = logArray[0];
    int i=1;
    /*@ loop_invariant
    @   0<=i && i <= logArray.length &&
    @   max!=null &&
    @   (\forall int j; 0 <= j && j<i;
    @     max.balance >= logArray[j].balance);
    @ assignable max, i;
    @ decreases logArray.length - i; */
    while(i<logArray.length){
        LogRecord lr = logArray[i++];
        if (lr.getBalance() > max.getBalance())
            max = lr;
    }
    return max;
}
```

# A Loop Example (Contd)



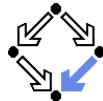
Press button "Start Proof".

# A Loop Example (Contd'2)



Press button "OK".

# A Loop Example (Contd'3)



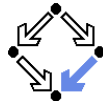
The screenshot shows the KeY Prover interface. The 'Tasks' pane on the left lists several goals, with 'EnsuresPost (paycard.LogFile.getMaximumRecord, ...)' selected. The 'Current Goal' pane on the right displays the following logical expression:

```
inReachableState
& \forallall paycard.LogFile p_0;
  (p_0.<created> = TRUE & lp_0 = null -> lp_0.logArray = null)
& \forallall paycard.LogFile p_0;
  (p_0.<created> = TRUE & lp_0 = null -> lp_0.a = null)
& \forallall paycard.LogFile p_0;
  (p_0.<created> = TRUE & lp_0 = null -> lp_0.b = null)
& \forallall paycard.LogFile p_0;
  (
    p_0.<created> = TRUE & lp_0 = null
    -> p_0.logArray.length = paycard.LogFile.logFileSize
      & ( p_0.currentRecord < paycard.LogFile.logFileSize
        & ( p_0.currentRecord >= (jint)0)
        & ( lp_0.logArray = null
          & \forallall jint i;
            ( 0 <= i & i <= p_0.logArray.length
              -> lp_0.logArray[i] = null))))))
& (self.<created> = TRUE & !self = null)
-> \<{
  exc=null;try {
    result=self.getMaximumRecord()@paycard.LogFile;
  } catch (java.lang.Throwable e) {
    exc=e;
  }
}> ( \forallall jint i;
  ( (jint)0 <= i & i < self.logArray.length & inInt(i)
    -> self.logArray[i].balance <= result.balance)
  & !result = null
  & exc = null)
```

The bottom status bar indicates 'Integrated Deductive Software Design: Ready'.

Press button "Start automated proof search".

# A Loop Example (Contd'4)

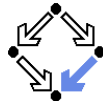


The screenshot shows the KeY Prover interface with the following components:

- Tasks:** A list of tasks including "EnsuresPost (paycard PayCard : charge, JML normal, ...)" and "EnsuresPost (paycard LogFile : getMaximumRecord, ...)".
- Proof Search Strategy:** A table with columns "Proof", "Goals", and "User Constraint".
- Open Goals:** A list of goals such as "self.logArray[i\_0].balance <= max\_0.balance,".
- Current Goal:** A large block of code representing the current goal state, including nested loops and conditional expressions. A yellow highlight is present on a portion of the code.
- Status Bar:** Displays "Strategy: Applied 1000 rules (3.3 sec, closed 18 goals, 3 remaining)".

Press button "Simplify".

# A Loop Example (Contd'5)



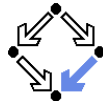
The screenshot shows the KQV Prover interface with the following components:

- Tasks:** A list of tasks including "EnsuresPost (paycard.PayCard::charge, JML normal...)" and "EnsuresPost (paycard.LogFile::getMaximumRecord,...)".
- Proof Search Strategy:** A table with columns for Proof, Goals, and User Constraint.
- Open Goals:** A list of goals, including "self.logArray[i\_0].balance <= max\_0.balance" and "self.logArray.<created> = TRUE, i\_2 <= 2, [b".
- Current Goal:** A large block of code defining a goal with nested loops and conditions, such as:

```
forall paycard.LogFile p_0;  
(p_0 = null | !p_0.<created> = TRUE | p_0.<currentRecord >= 0),  
forall paycard.LogFile p_0;  
(p_0 = null | !p_0.<created> = TRUE | p_0.<currentRecord <= 2),  
self.logArray.length = 3,  
forall paycard.LogFile p_0;  
(p_0 = null | !p_0.<created> = TRUE | p_0.logArray.length = 3),  
forall paycard.LogFile p_0;  
forall jint i;  
( i <= -1  
 | p_0 = null  
 | !p_0.<created> = TRUE  
 | self.logArray[i_0].balance <= max_0.balance  
 | self.logArray.<created> = TRUE  
 | inReachableState))
```
- Information Dialog:** A small dialog box with the message "1 goal has been closed" and an "OK" button.
- Status Bar:** A message at the bottom reads "SIMPLIFY: 3 goals processed, 1 goal could be closed".

Press button "Start automated proof search".

# A Loop Example (Contd'6)



Tasks

- EnsuresPost (paycard PayCard::charge, JML normal, b...
- with model paycard@10:00:47 AM #2
- EnsuresPost (paycard LogFile::getMaximumRecord, p...

Proof Search Strategy

Rules

User Constraint

Open Goals

Inner Node

```
( p_u = null
  | p_0.<created> = TRUE
  | p_0.logArray.length = 3),
\forall\forall\forall paycard.LogFile p_0;
\forall\forall\forall jint i;
( i <= -1
  | p_0 = null
  | p_0.<created> = TRUE
  | p_0.logArray.length <= -1 + i
  | p_0.logArray[i] = null),
self.<created> = TRUE
```

Proof closed

Proved.

Statistics:

Nodes:1374

Branches: 26

OK

```
non_0(i, max)
...
& ( self.logArray.length >= (jint)(1 + i_0)
  & ( !max_0 = null
    & ( !max_0.<created> = TRUE
      & \forall\forall\forall jint j;
        ( j <= -1
          | j >= (jint)(1 + i_0)
          | self.logArray[j].balance
            <= max_0.balance))))
& inReachableState))
```

Node Nr 1021

Upcoming rule application:

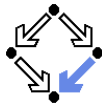
```
concrete_and_1 {
```

KIV Strategy: Applied 348 rules (1.1 seq, closed 8 goals, 0 remaining)

Verification is successful.



# Summary



- Various academic approaches to verifying Java(Card) programs.
  - Jack: <http://www-sop.inria.fr/everest/soft/Jack/jack.html>
  - Jive: <http://www.sct.ethz.ch/research/jive>
  - Mobius: <http://kind.ucd.ie/products/opensource/Mobius>
- Do not yet scale to verification of large Java applications.
  - General language/program model is too complex.
  - Simplifying assumptions about program may be made.
  - Possibly only special properties may be verified.
- Nevertheless helpful for reasoning on Java in the small.
  - Beyond Hoare calculus on programs in toy languages.
- Enforce clearer understanding of language features.
  - Perhaps constructs with complex reasoning are not a good idea...
- Trend: modularization of reasoning.

In a not too distant future, customers might demand that some critical code is shipped with formal certificates (correctness proofs)...